Benchmarking and Simulating the CBETA FFAG Arc Cell

Muon1 Simulations Stephen Brooks
Lattice Design Scott Berg

CBETA FFAG Arc Cell Lattice

Table 2.6.1: Hard edge arc cell design parameters.

Injection Total Energy (MeV)	6	
Maximum Total Energy (MeV)	150	
Linac Passes	4	
Reference Radius (m)	5.099439	
L_{DF} (mm)	120	
L_{FD} (mm)	70	
α	F	D
$L_{Q\alpha}$ (mm)	133	122
x_α (mm)	−7.182	+20.132
Gradient (T/m)	+10.621	−10.017

Table 2.6.2: Horizontal displacements for the real magnets, determined using field maps.

x_F (mm)	−4.089
x_D (mm)	+17.313

Code Comparison

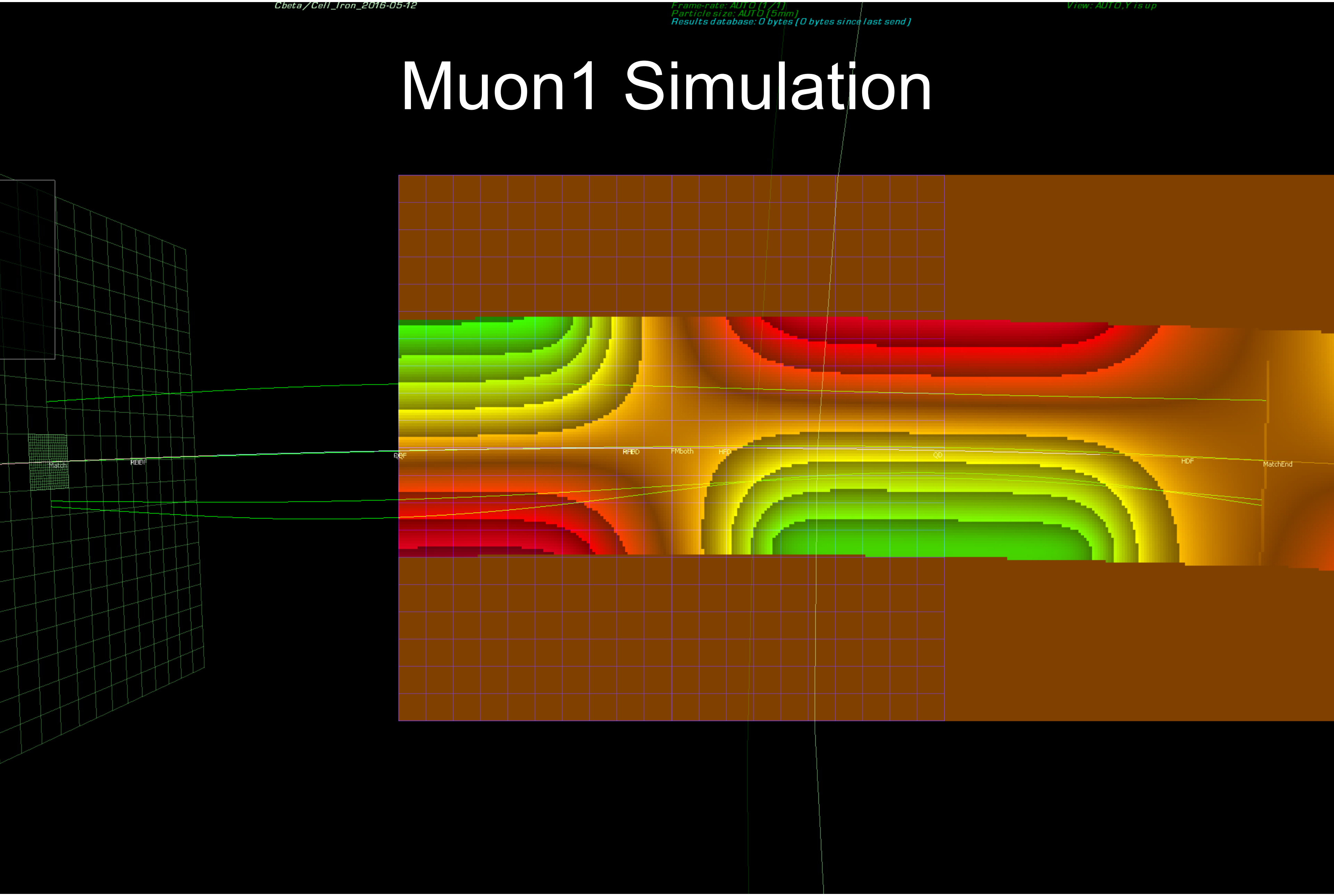
Muon1 (by Stephen Brooks)

- Uses Cartesian global-frame coordinates
- Tracks in t
- Runge-Kutta 4th order
- Fixed timestep of 10ps (I sometimes lower this to 5ps for CBETA, very little difference)
- Fieldmaps are interpolated trilinearly (occasionally leads to rough edges when finding tunes)

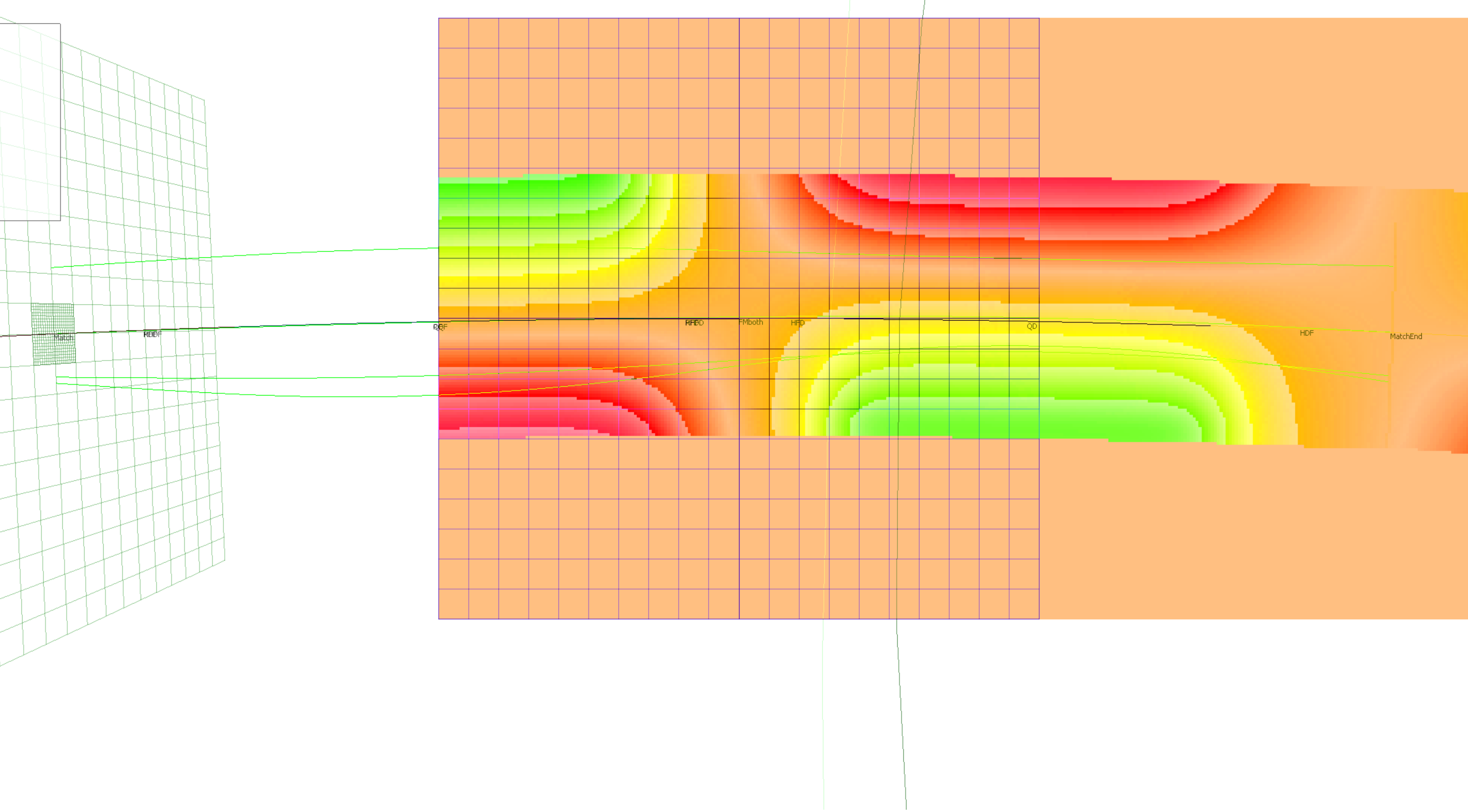
"Scott's Code" (developed recently for CBETA)

- Uses cylindrical polar coordinates (r,theta,y)
- Tracks in theta
- Also Runge-Kutta 4th order
- Fieldmaps are fitted with smooth splines and particles are tracked through the spline fit

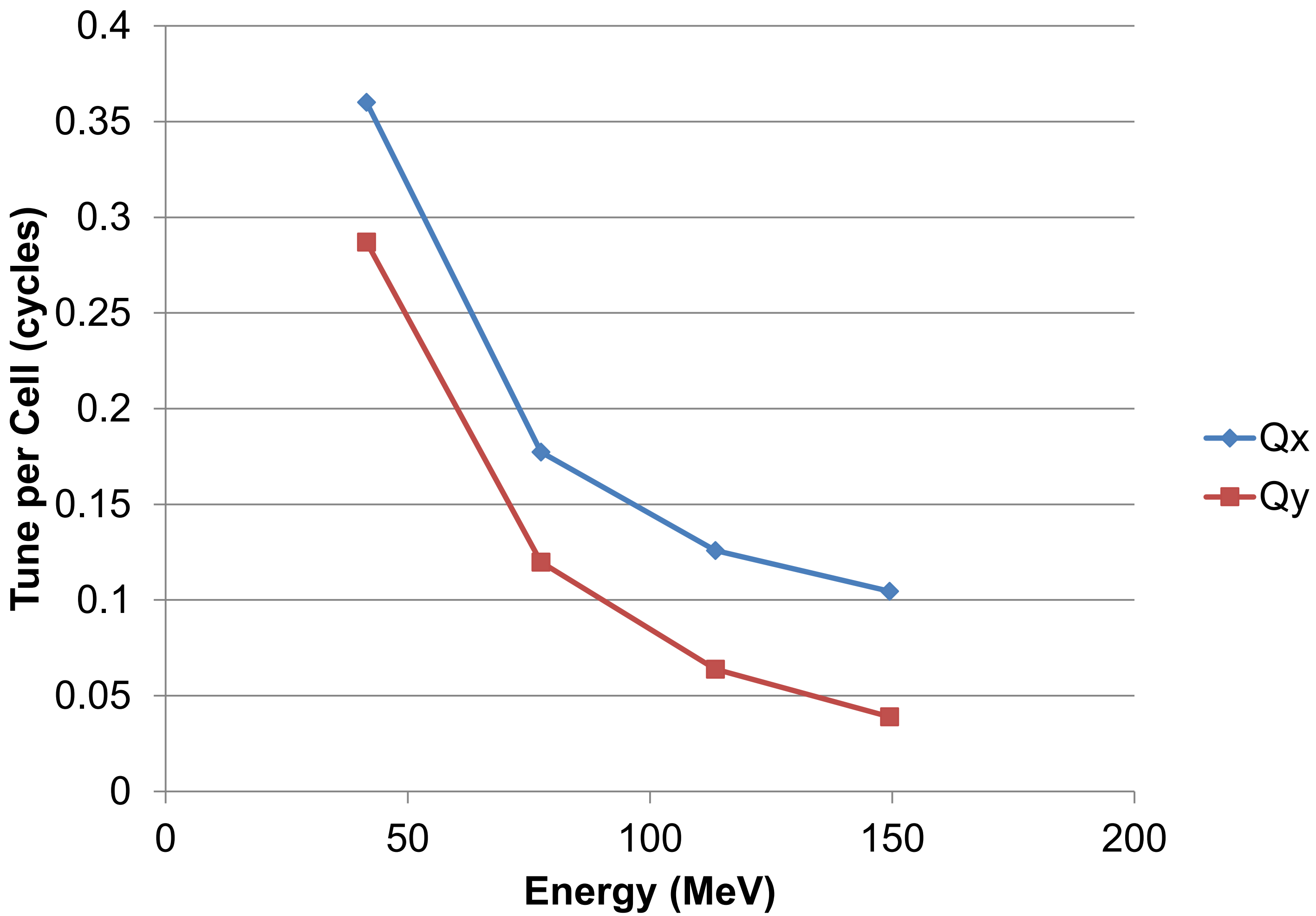
Muon1 Simulation



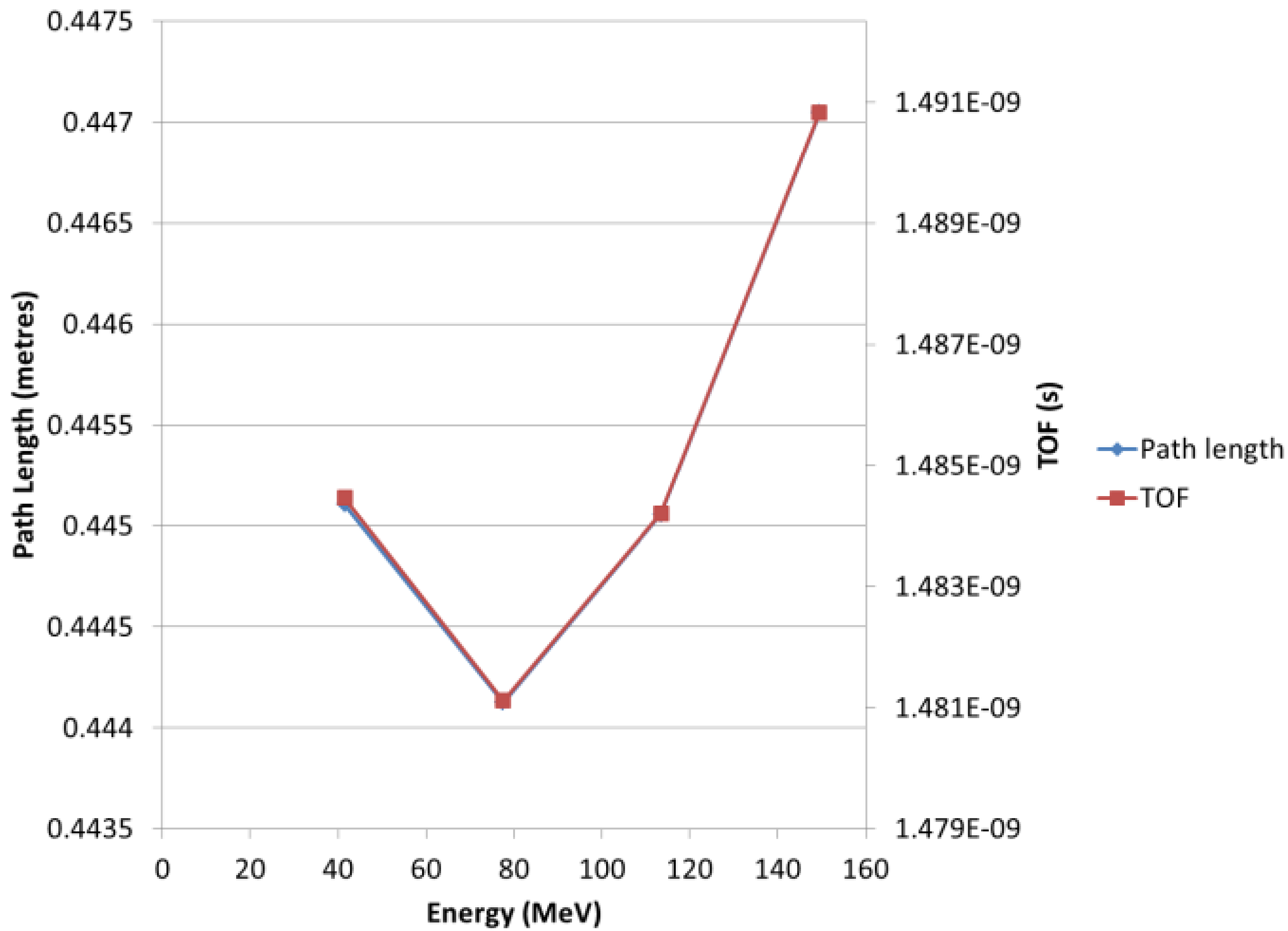
Muon1 Simulation



Cell Tunes from Muon1



Cell Path Length and TOF



Cell Tunes from Both Codes

Total Energy (MeV)	Muon1 Cell Tune X	Muon1 Cell Tune Y	Scott Cell Tune X	Scott Cell Tune Y
42	0.360041	0.286975	0.363443	0.289387
78	0.177298	0.119886	0.178187	0.120718
114	0.125858	0.0638703	0.126546	0.0644552
150	0.104551	0.0390379	0.105049	0.0399600

Only the first turn (42MeV) is in the region susceptible to strong resonances. The rest of the turns are in the pseudo-continuous phase advance regime.

The low tune is always the Y tune at the highest energy. Going higher makes it difficult to find a lattice with practical field strengths. Going lower makes optics sensitive to focussing errors and not enough phase advance for "adiabatic" transition from FFAG arc to straight.

Scott Berg's CBETA FFAG Arc Cell (and Holger's Fieldmaps) Imported Into Muon1

File "Cbeta/Cell_Iron_2016-05-12"

```
{Scott's 150MeV lattice from "160507-JSBerg" folder, using Holger's
fieldmaps from "160512-FieldMap" subfolder}

#h   = +1.9610000439244032e-01;
#R=1.0/h;

#lqf  = +1.3300000000000001e-01;
#lqd  = +1.2200000000000000e-01;
#lfd  = +7.0000000000000007e-02;
#ldf  = +1.2000000000000000e-01;

#thqf=2*asin(0.5*lqf/R);
#thqd=2*asin(0.5*lqd/R);
#thfd=2*asin(0.5*lfd/R);
#thdf=2*asin(0.5*ldf/R);

{Drift Length Angle}
DF #R*thdf# #thdf*-1#
QF #R*thqf# #thqf*-1#
FD #R*thfd# #thfd*-1#
QD #R*thqd# #thqd*-1#
HDF #DF.Length/2# #DF.Angle/2#
HFD #FD.Length/2# #FD.Angle/2#
```

Scott's parameters
h is inverse radius

Convert chord lengths to arc lengths

Define empty circular arc elements (radius R) for layout reference

Half-elements

```
#scalboth = 1; dispboth = 0;
#scalF = 1; scalD = 1;
#dispF = 0; dispD = 0;

{TrilinearFieldMap File Strength Xrel MirrorY=1}
FMboth Cbeta\Iron_2016-05-12\160308a-38-
48_5deg150MeVCombQdOnQfOn_polar.txt #scalboth*-1# #dispboth-
R#
FMF Cbeta\Iron_2016-05-12\160308a-38-
48_5deg150MeVSepQfOn_polar.txt #scalF*-1# #dispF-R#
FMD Cbeta\Iron_2016-05-12\160308a-38-
48_5deg150MeVSepQdOn_polar.txt #scalD*-1# #dispD-R#

CellFM: HDF,QF,HFD,FMboth,HFD,QD,HDF;
CellFMsep: HDF,QF,HFD,FMF,FMD,HFD,QD,HDF;

#Emin = +4.2000000000000000e+07;
#Emax = +1.5000000000000000e+08;
#n    = 4;

#EmasseV=510998.928;
{MatchScan Estart Egoal Estep Species=Electron AllowUnstable=1}
Match #Emax-EmasseV#eV #Emin-EmasseV#eV #(Emax-Emin)/(n-
1)#eV
MatchFine #Match.Estart# #Match.Egoal# 1MeV

{Match-Aperture}
MatchEnd

CellFM,Match,CellFM,MatchEnd,CellFM;
```

No scaling or displacement for final fieldmap version

Fieldmaps

Cell definitions

Scott's energy range
Number of passes
Units, total E. -> k.e.

Place 3 cells to allow fringe field overlaps

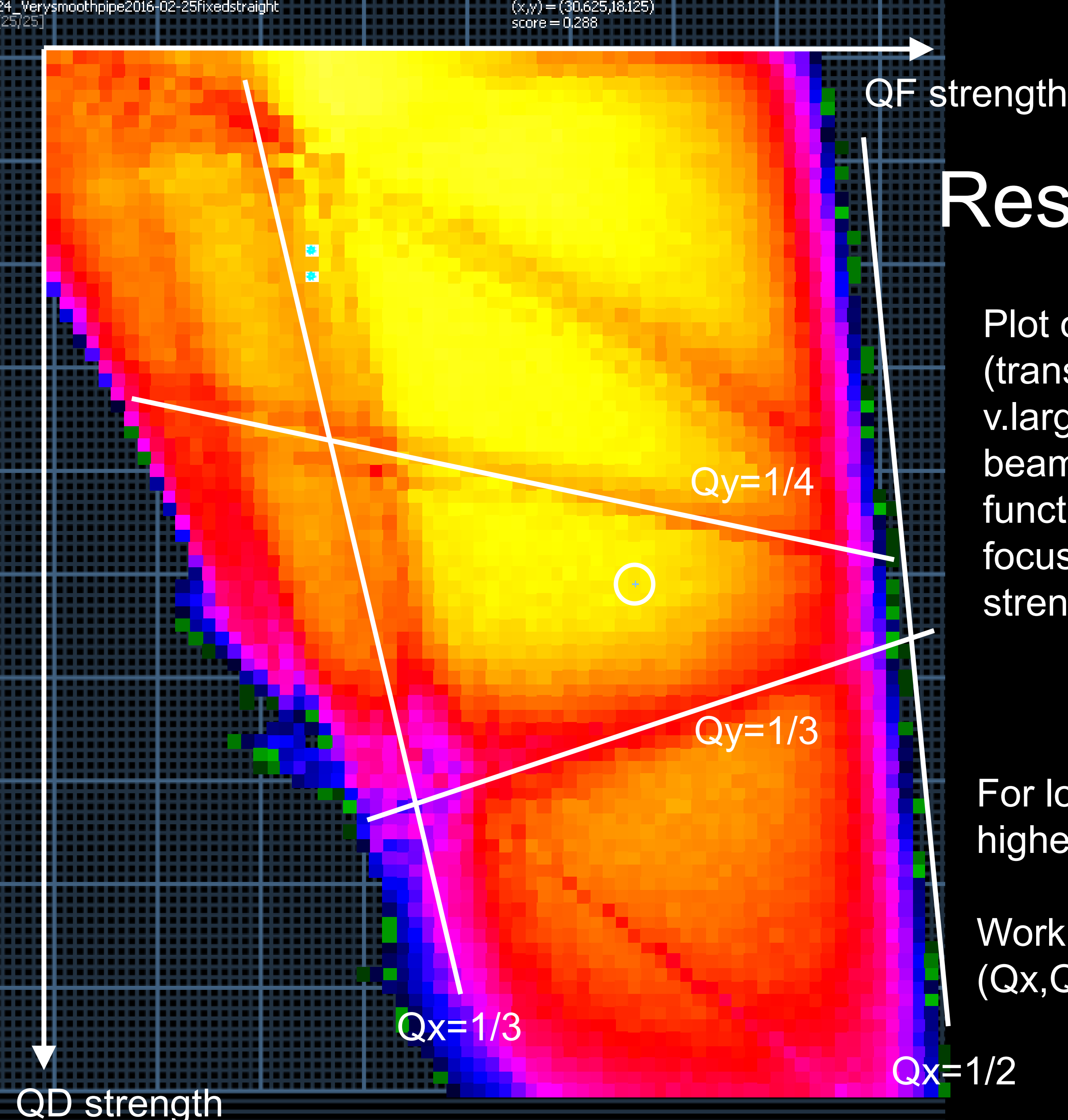
Focus: Aligning the Fieldmaps

```
{TrilinearFieldMap File Strength Xrel MirrorY=1}
FMboth Cbeta\Iron_2016-05-12\160308a-38-48_5deg150MeVCombQdOnQfOn_polar.txt #scalboth*-1# #dispboth-R#
FMF Cbeta\Iron_2016-05-12\160308a-38-48_5deg150MeVSepQfOn_polar.txt #scalF*-1# #dispF-R#
FMD Cbeta\Iron_2016-05-12\160308a-38-48_5deg150MeVSepQdOn_polar.txt #scalD*-1# #dispD-R#
```

3 fieldmaps with long file names
Field magnitude is inverted due to difference in curvature direction (Scott vs. reality)
Relative position in local X is “-R”, i.e. origin is centre of radius R circle
Mirrored in Y to give both positive and negative Y

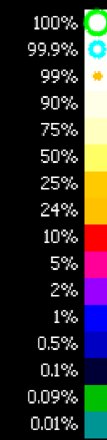
```
CellFM: HDF,QF,HFD,FMboth,HFD,QD,HDF;
CellFMsep: HDF,QF,HFD,FMF,FMD,HFD,QD,HDF;
```

For each version of the cell (combined or separate fieldmaps), the maps are placed at the centre of the F-to-D (short) drift
The cell entrance/exit is the centre of the D-to-F (long) drift



Resonance Plot

Plot of aperture (transmission of v.large 1cm-radius beam) as a function of two focussing strengths

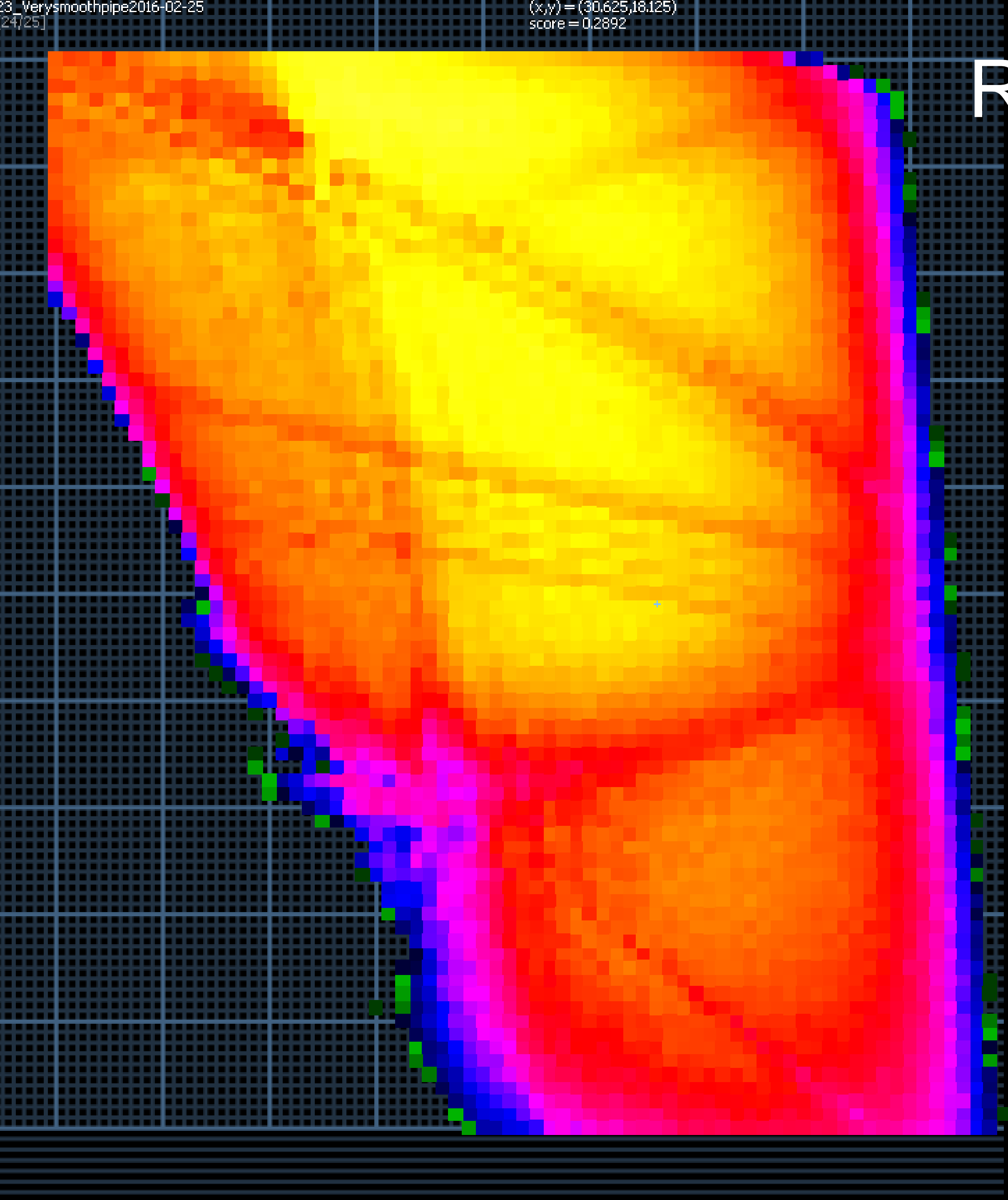


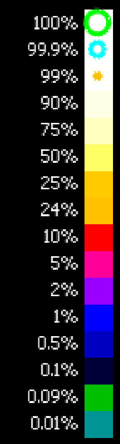
For lowest-energy pass, highest tunes.

Working point circled: (Qx,Qy) = (0.360,0.287)

Resonance Plot

before adjustment to straight drift lengths





Resonance band features broadened because straight section has different tunes to arcs. Can fix by adjusting straight section drift lengths.

Conclusions

- The CBETA FFAG has been simulated in Scott's code, Muon1 and BMAD
- These codes have very different internal operation yet we get consistent results
- Arc-to-straight match has been optimised for an old lattice, currently being optimised for the newest version