

# Potential and Issues for Future Accelerators and Ultimate Colliders

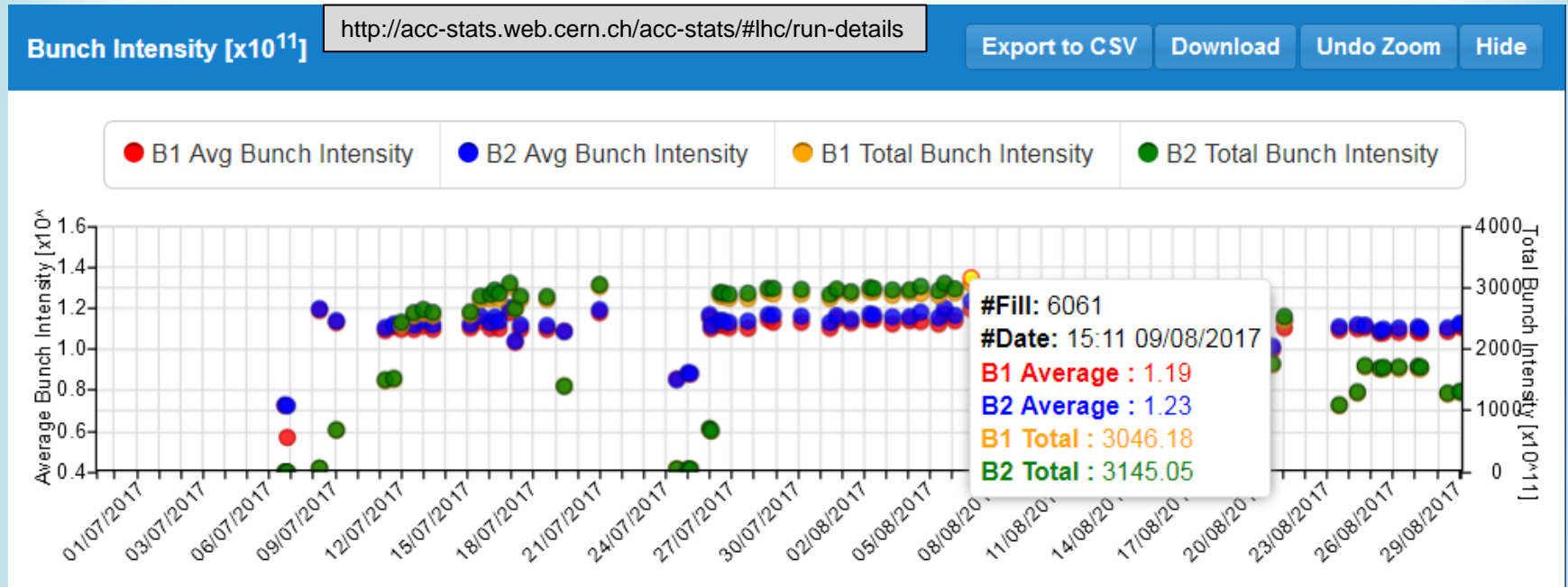
Including a few things from the “F3iA 2016” meeting in Germany  
(look it up for others’ perspectives)

<https://indico.desy.de/indico/event/15657/>

# Energy Frontier

- What if there is no easy new physics and a large “energy desert” to cross?
- Let’s examine an extreme example and see what could be different about energy frontier machines in the far future that are capable of discovering new physics
  - Context for the F3iA meeting was “accelerators in the 2<sup>nd</sup> half of the 21<sup>st</sup> century”
  - What I describe here could be even further out

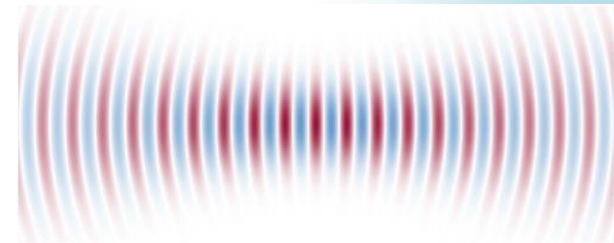
# The Case for Optimism



- $2 * 3.1e14 * 6500 \text{ GeV} = 645 \text{ MJ} = 0.33 E_{\text{Planck}}$
- Total energy is OK but in too many particles
  - Maybe we should try 1 particle per beam?

# Single-Particle Accelerators

- Wavefunction propagates through lattice
  - Can still form optical foci like with laser photons
  - Minimum emittance  $\varepsilon_{N,rms} = \hbar/2mc$  set by uncertainty principle
- Need emerging ultra-cold and precision alignment technology
  - Unfamiliar areas for us!



## Experiment example:

Put single particles with quantum behaviour (e.g. from “double slit”) through accelerator-type optics and final focus

## Collaboration with:

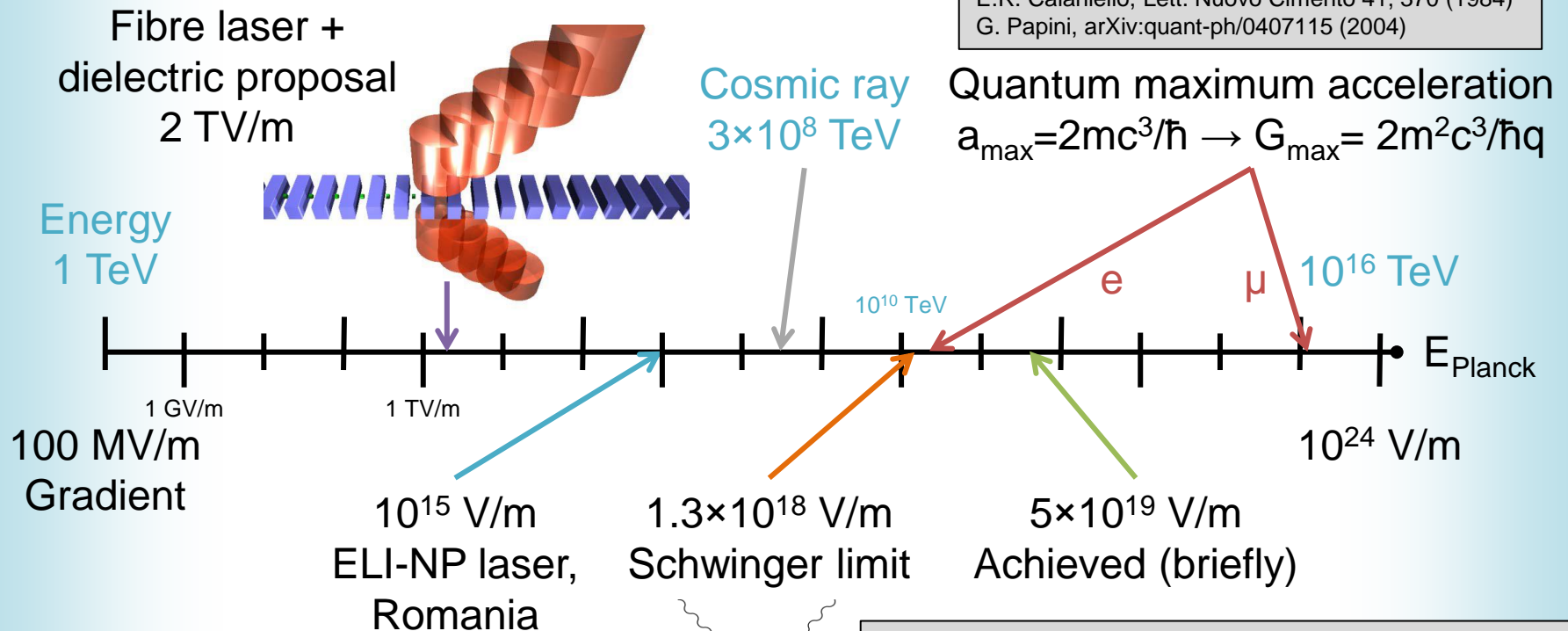
Atomic physics  
Quantum computing  
Ultra-cold physics  
Metrology  
Gravitational wave detection



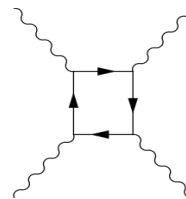
# Gradients in a 2×10km-long Facility

A. Pukhov *et al.*, Eur. Phys. J. ST 223, 1197–1206 (2014)

E.R. Caianiello, Lett. Nuovo Cimento 41, 370 (1984)  
G. Papini, arXiv:quant-ph/0407115 (2004)



At  $\sim 10^{18}$  V/m gradient, would need  $\sim 10$  million km to get to the Planck energy. Or can we do something about that? In 10km.



*On a Diffuse Reflection of the  $\alpha$ -Particles.*

By H. GEIGER, Ph.D., John Harling Fellow, and E. MARSDEN, Hatfield Scholar, University of Manchester.

(Communicated by Prof. E. Rutherford, F.R.S. Received May 19,—Read June 17, 1909.)

# Shortcut to Planck scale: Black Hole

M.W. Choptuik and F. Pretorius, Phys. Rev. Lett. 104, 111101 (2010)

- Black holes can form from k.e. in collisions
  - Schwarzschild radius scales linearly with mass
  - Instead of putting  $1 E_{\text{Planck}}$  in  $1 L_{\text{Planck}}$  ...  $r_s = 2GM/c^2$
  - Put  $10^6 E_{\text{Planck}}$  in  $10^6 L_{\text{Planck}}$
- Need a diffraction-limited focus of  $10^{12}$  particles at  $10^{10}$  TeV (instead of 2 at  $10^{16}$  TeV)
  - Energy requirement goes up by  $10^6$  to 893 GW.h
    - Large but not a show-stopper in the long run

If we don't make a black hole (e.g. in the case of Einstein-Cartan theory), that's OK, we've still probed new physics

# Black Hole Factory Parameter Table

Parameter	Bosons e.g. photons (overlapping)	Fermions or non-overlapping bosons
Energy	$10^{10}$ TeV	$10^{12}$ TeV
Length	10 km	1000 km (space)
Gradient	$10^{18}$ V/m	$10^{18}$ V/m
Number of particles	$10^{12}$	$10^{12}$
Total energy per pulse	$3.22 \times 10^{15}$ J = 893 GW.h	$3.22 \times 10^{17}$ J = 89.3 TW.h
Repetition period	14 days	14 days
Average power	2.66 GW	266 GW
$\sigma_x^* = \sigma_y^* = \sigma_z^*$	$1.97 \times 10^{-29}$ m	$1.97 \times 10^{-27}$ m (beam)
$\sigma_\theta^* = \sigma_E^*/E$	0.5 rad = 50%	0.5 rad = 50%
Black hole radius = $2.14\sigma_x^*$	$4.22 \times 10^{-29}$ m	$4.22 \times 10^{-27}$ m
Black hole mass	28.4 grams	2.84 kg
Black hole lifetime	$1.10 \times 10^{-22}$ s (evaporation)	$1.10 \times 10^{-16}$ s

Deepest mine=4km,  
allows +/-226km  
laterally within Earth

worse

\$107M per shot at US  
avg. electricity price

worse

By far the hardest  
parameters are the  
alignment & emittance

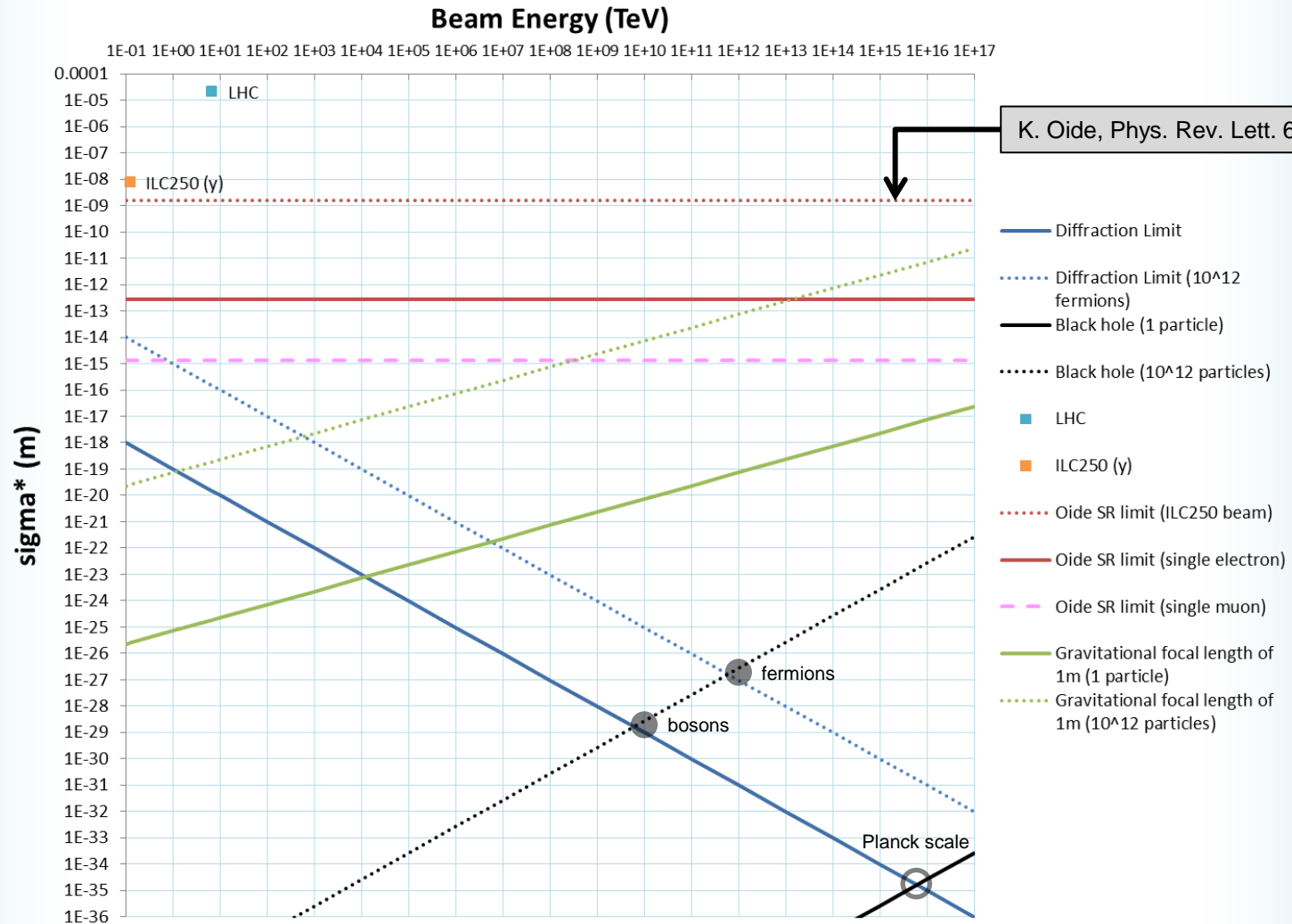
6D phase space  
N times larger,  
 $N^{1/3}$  each plane



# Compare at 100km Length

Parameter	Bosons e.g. photons (overlapping)	Fermions or non-overlapping bosons
Energy	$10^{11}$ TeV	$10^{11}$ TeV
Length	100 km	100 km
Gradient	$10^{18}$ V/m	$10^{18}$ V/m
Number of particles	$10^{10}$ <span>better</span>	$10^{15}$ <span>way worse</span>
Total energy per pulse	$3.22 \times 10^{14}$ J = 89.3 GW.h	$3.22 \times 10^{19}$ J = 8.93 PW.h
Repetition period	14 days <span>\$10.7M per shot at US avg. electricity price</span>	14 days
Average power	266 MW <span>better</span>	26.6 TW <span>way worse</span>
$\sigma_x^* = \sigma_y^* = \sigma_z^*$	$1.97 \times 10^{-30}$ m	$1.97 \times 10^{-25}$ m (beam)
$\sigma_\theta^* = \sigma_E^*/E$	0.5 rad = 50%	0.5 rad = 50%
Black hole radius = $2.14\sigma_x^*$	$4.22 \times 10^{-30}$ m	$4.22 \times 10^{-25}$ m
Black hole mass	2.84 grams	284 kg
Black hole lifetime	$1.10 \times 10^{-25}$ s	$1.10 \times 10^{-10}$ s

# Energy vs. Focus Size



K. Oide, Phys. Rev. Lett. 61, 1713 (1988)

# Limit? Emittance Growth from SR

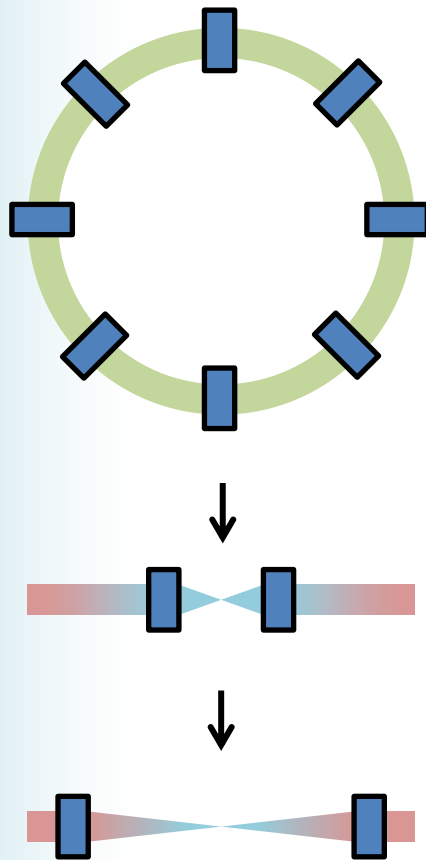
- Oide's bound depends only on  $\epsilon_N$

K. Oide, Phys. Rev. Lett. 61, 1713 (1988)

$$\sigma_{y\min}^* = \left(\frac{7}{5}\right)^{1/2} \left[ \frac{275}{3\sqrt{6}\pi} r_e \lambda_e F(\sqrt{K}L, \sqrt{K}l^*) \right]^{1/7} (\epsilon_{Ny})^{5/7}$$

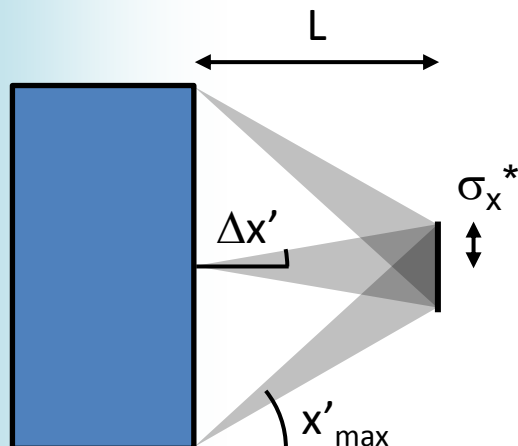
- The final focus magnets themselves cause synchrotron radiation emission and scattering
- Exceptions to the assumptions of this formula:
  - (A) Bending happens at lower energy than focus
  - (B) Quantum effects (coherence, entanglement)
  - (C) Non-electromagnetic focussing

# (A) Even Linearer Colliders

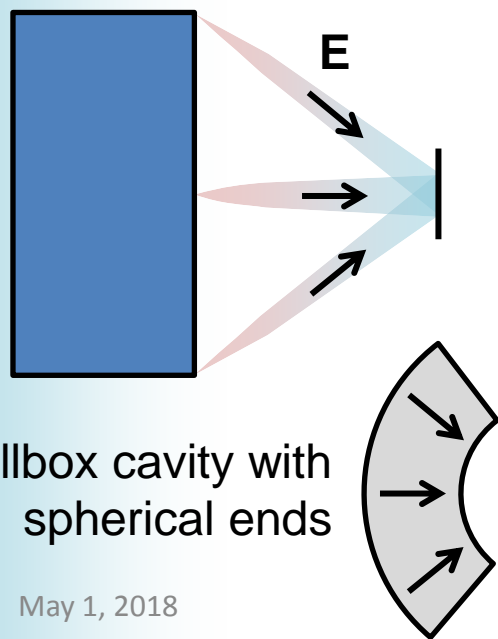


- Rings bend 360 degrees per turn up to highest energy
- Linear colliders bend by  $\sim$ mrads at highest energy
- Bend at lowest energy and then accelerate afterwards?

# (A) Beyond the Lower Bound



- Consider the optimised focus
- Bend in magnet is  $x'_{\max}$
- Now add **E**-field parallel to trajectories, reduces  $\Delta x'$
- Bend in **E**-field only  $\Delta x' = \sigma_x^*/L$ 
  - Can make this arbitrarily small, so not a significant source of SR



Pillbox cavity with spherical ends

## Experiment:

Can we break K. Oide's lower bound on focus size in the lab?

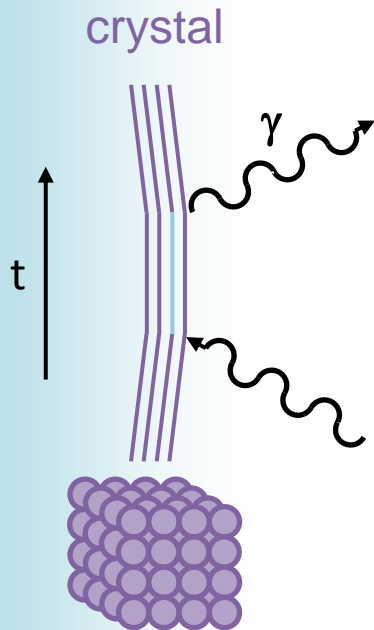
# (B) The Problem in Quantum Terms

- Is there an initial state that...
  - Forms a black hole on a reasonable time-scale
  - No high energy particles, total size  $R < 10\text{km}$ , total mass-energy and density  $\sim$  everyday objects?
- Answer: yes
  - Construction: take the state just before Planck black hole formation and track backwards in time using CPT theorem, particles hit walls, produce showers, eventually a few MJ-GJ of energy absorbed; result: warm concrete walls
- This state is entangled in a very particular way
  - Also applies to Mössbauer accelerators

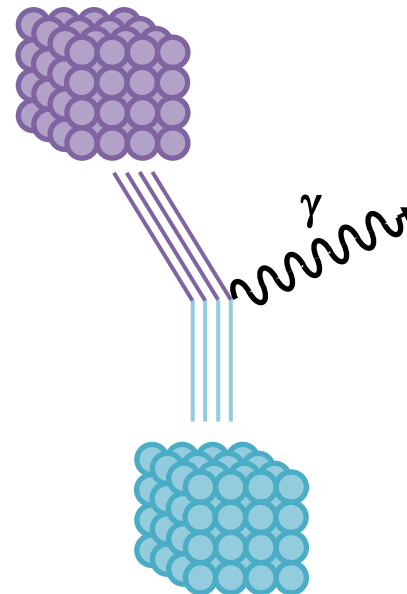
# (B) Mössbauer Accelerator

R.L. Mössbauer, Z. Physik 151, 124 (1958)  
P.P. Craig *et al.*, Phys. Rev. Lett. 3, 221–223 (1959)

A.-S. Müller, talk at F3iA 2016 meeting



Mössbauer effect:  
Gamma ray from  
nuclear excitation  
recoils against the  
entire mass of the  
crystal, giving  
very low energy  
spread



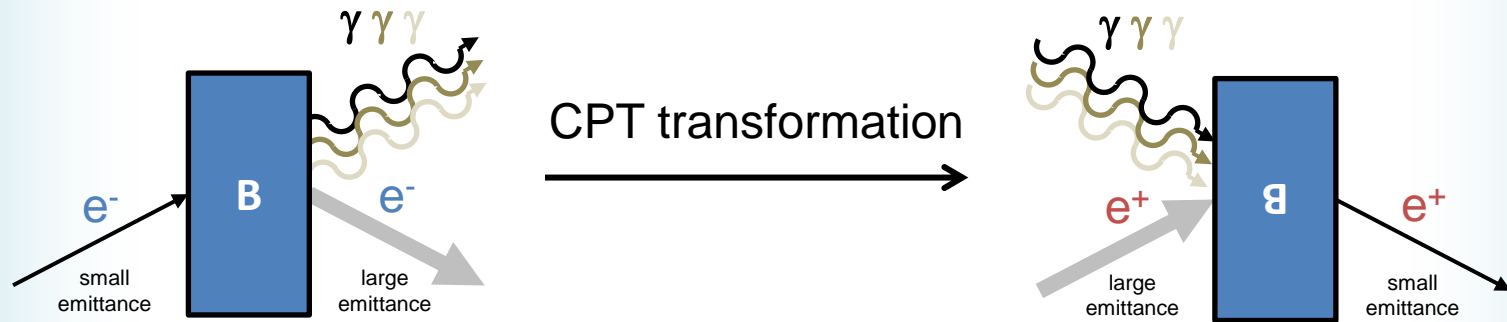
If many nuclei are  
excited, could the  
entire energy be  
transferred to a  
single emitted  
particle, since the  
crystal is acting  
coherently?

E.g.  $^{191}\text{Ir}^*$  emits 129keV gamma rays, a macroscopic crystal  
of  $9.5 \times 10^{22}$  iridium atoms (30 grams) could emit  $E_{\text{Planck}}$

F. Vagizov *et al.*, “Coherent control of  
the waveforms of recoilless  $\gamma$ -ray  
photons”, Nature 508, 80–83 (2014)

← Another useful application: modulating the wavefunction  
of a single gamma photon using the Doppler shift

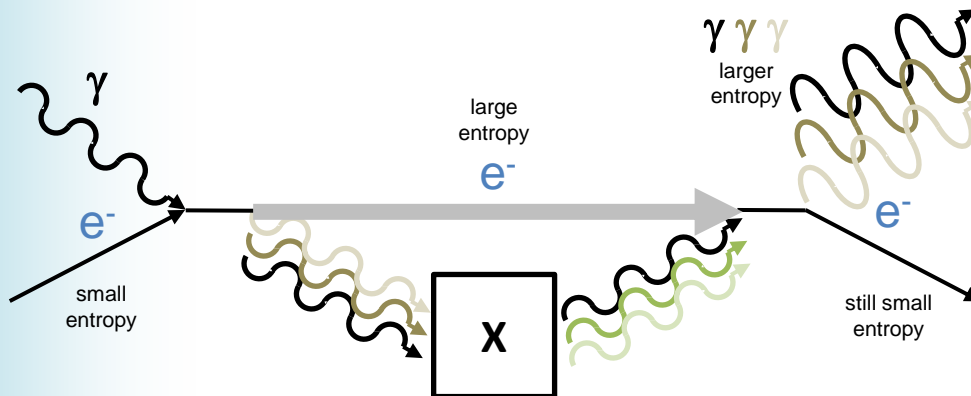
# (B) Time Reversal of SR Emission



There are some quantum scenarios where emittance growth from SR can be stopped or even reversed. Below is a generic “cooling” system.

## Experiment:

Can we make the photon state in the diagram above? NB: it's probably entangled with the input positron



## Simulation/experiment:

Does such a process X exist and it be realised?



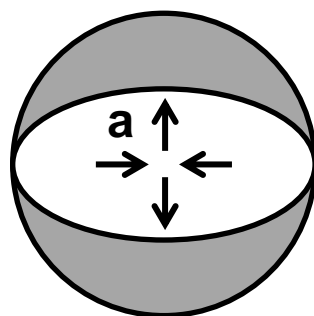
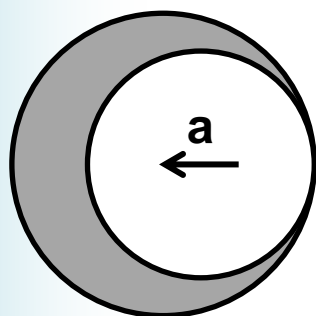
# (B) Unused Degrees of Freedom

- Non-thermal distributions of particles
- Control of particle wavefunctions
  - Beam particle(s)
  - Accelerating photons (RF/laser)
- Entanglement
  - Between beam particles
  - Between beam and RF/laser
  - Between RF/laser and itself

As experimenters, we make **both** the beam and the accelerating photons, so no reason why this is not allowed

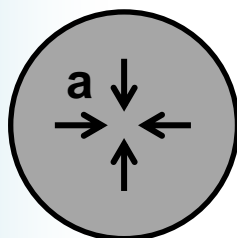
## (C) Gravitational Final Focus

- If you can make a black hole, you can make a gravitational lens at lower densities
  - Use it to help reduce opening angle of final focus



2D, completely-linear gravitational dipole and quadrupole, based on subtracting two K-V distributions of mass

No synchrotron radiation emitted because gravity redefines what a “straight line” is



Linear “monopole” focussing lens also possible but the beams would collide! A shame because two interpenetrating KV beams would self-focus analogous to high intensity e-p IRs

## (C) Simplified Calculation

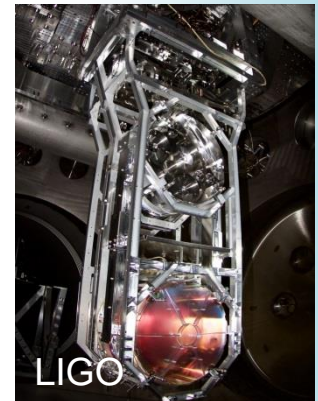
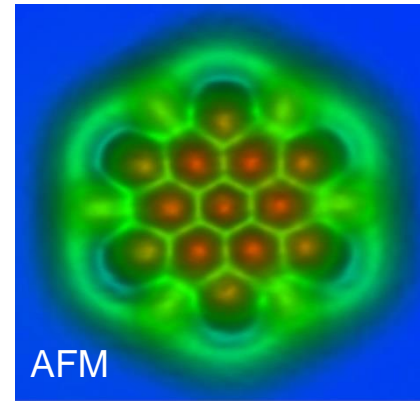
- Assume you only have  $\sigma_{\theta}^* = 0.5/N$  rad ( $N \times$  low)
  - So can only make  $\sigma_x^*$   $N \times$  that needed for BH
- Deflection from lensing  $\theta = 2r_s/r = 2/N$  rad
  - So need at least  $0.5/(2/N) = N/4$  times the mass
- Extra mass required scales up as inverse of originally achievable  $\sigma_{\theta}^*$ 
  - Particles forming lenses do not create black hole
    - So candidates for energy recovery

# Nucleus-Level Alignment?

Nearer-term experiments

Collaboration with:  
Nanotechnology, fusion(?)

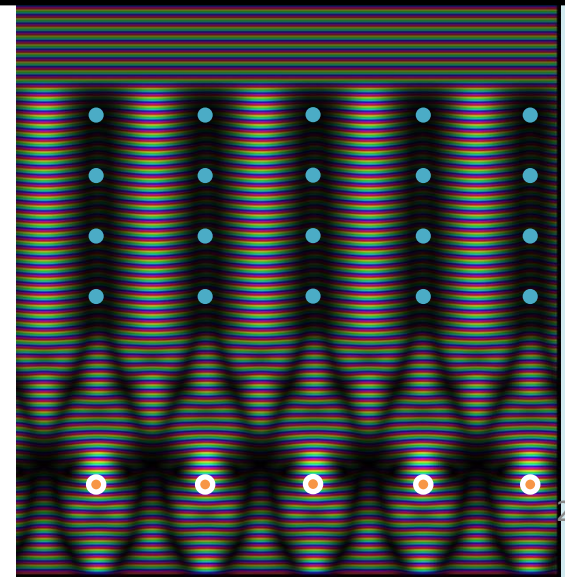
- Can we demonstrate changing a nuclear reaction rate by a spatial/positioning effect?
  - AFM tip  $\leq 5 \times 10^{-11}$  m
  - LIGO mirrors  $\sim 10^{-16}$  m
    - Measurement  $\sim 10^{-18}$  m
- Or could use crystal channelling alignment



XY Scanner

Single module flexure XY-scanner with closed-loop control  
50  $\mu\text{m}$   $\times$  50  $\mu\text{m}$  (optional 10  $\mu\text{m}$   $\times$  10  $\mu\text{m}$  or 100  $\mu\text{m}$   $\times$  100  $\mu\text{m}$ )  
Resolution : 0.05 nm  
Position detector noise : < 0.25 nm (bandwidth: 1 kHz)  
Out-of-plane motion : < 2 nm (over 40  $\mu\text{m}$  scan)

Park NX10



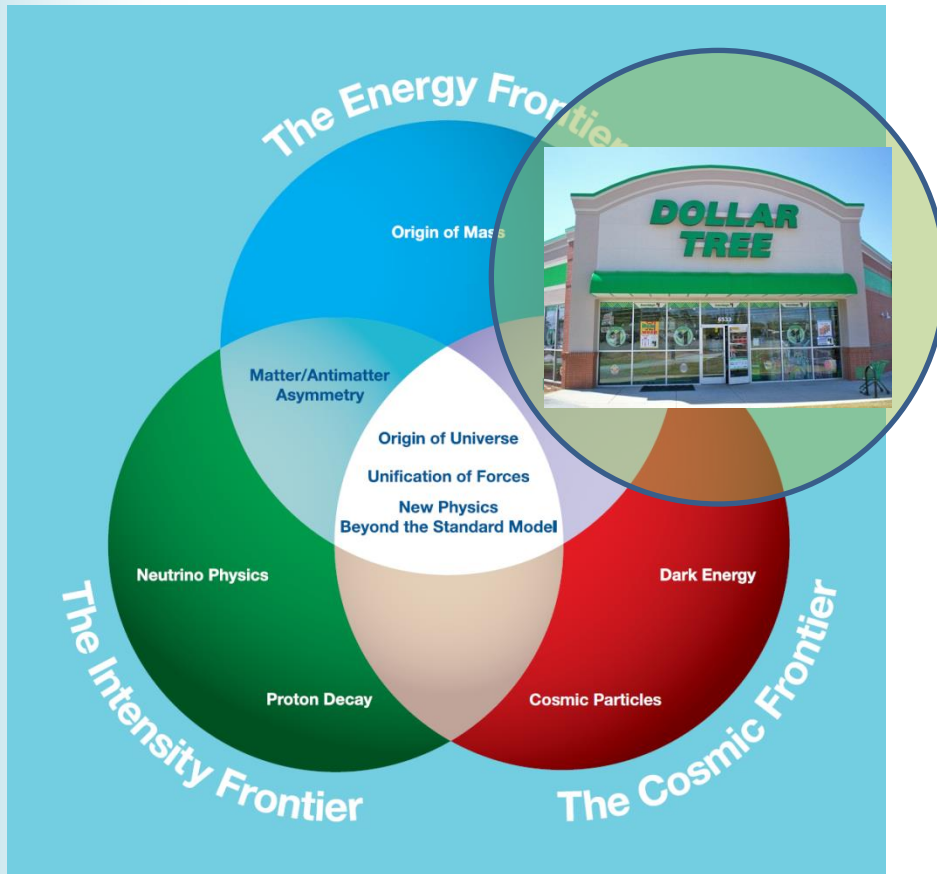
# Summary: Single-Particle Collider

- Currently, we collide a billion+ particle bunch and get  $\sim 10$  events per crossing
  - Somehow a  $>10^8$  factor in efficiency has been lost
  - Various factors to blame: with 20<sup>th</sup> century technology this was the only way to get it to work
    - And it's still hard
    - But big reward
      - e.g. LC power limit
- There is no intra-beam scattering if you only have one particle per bunch

## Experiment:

Apparatus to collide particles individually, then gradually increase accelerating voltage

# Cheapness Frontier



## Mass-produced parts

- Benefit from other industries

## Don't over-spec

- Evade precision requirements by staging and feedback

## Automation

- Manpower will be the most expensive item in the future
- 3D printing, robotics
- AI / automated design

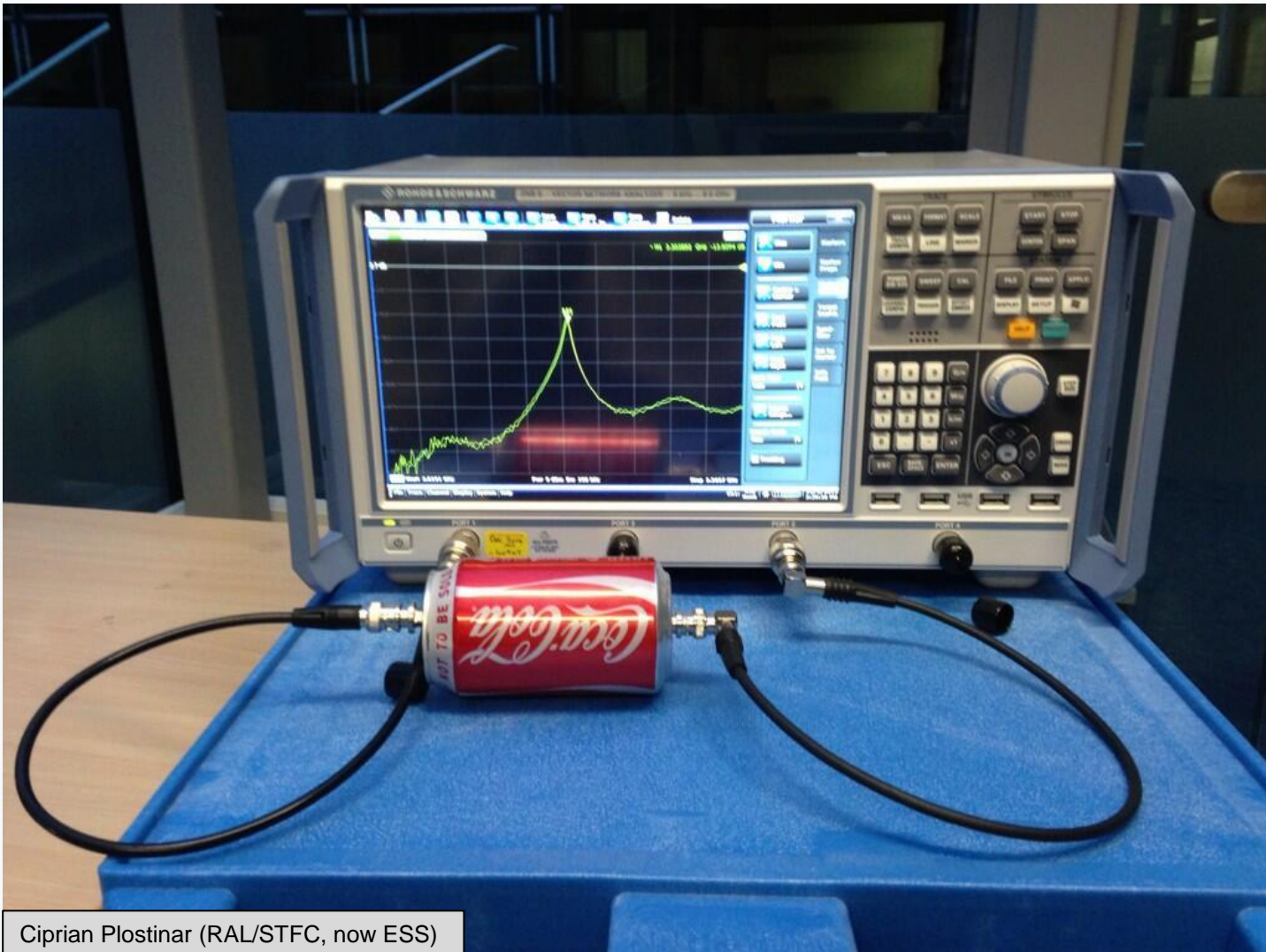
## Recycling

- Energy recovery, multi-pass

- Why? Since accelerators are already at the limits of government research budgets



$$f = 3.3 \text{ GHz}, Q = 50$$



Ciprian Plostinar (RAL/STFC, now ESS)

$$f = 150\text{--}165 \text{ MHz}, Q = 9700$$

GERALD DAVID OBE FREng  
AERIAL FACILITIES LTD

DESIGN AND TECHNOLOGY

The unloaded  $Q_0$  obtained in practice at 150 MHz exceeded 9000 and in very carefully prepared cavities figures up to 9700 could be obtained.

we did not come across any significant problems due to the casting or welding so the quality of the conductivity was of the highest order. The other great advantage of this device was the price which, in the raw form, was £47 per barrel when ordered in quantities of 100.

# The beer barrel as a VHF cavity resonator

*In the 1970s, use of mobile radio frequencies was expanding dramatically and existing antennas were becoming heavily overloaded. The engineering solution devised by Gerald David was to introduce multiple transmitter combiners onto a single antenna using band-pass filters. The use of a beer barrel in this context shows how existing structures can be adapted to new uses at a fraction of the cost of purposely designed components.*



G. David, Ingenia Magazine 18, 21–25 (2004)



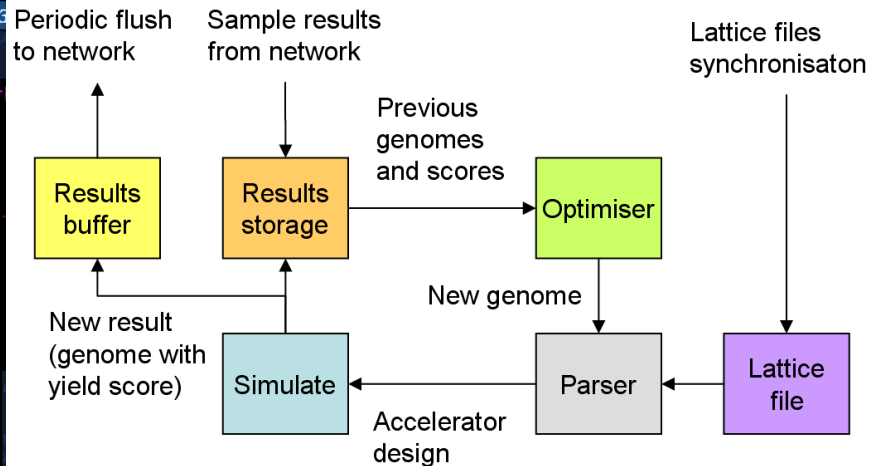
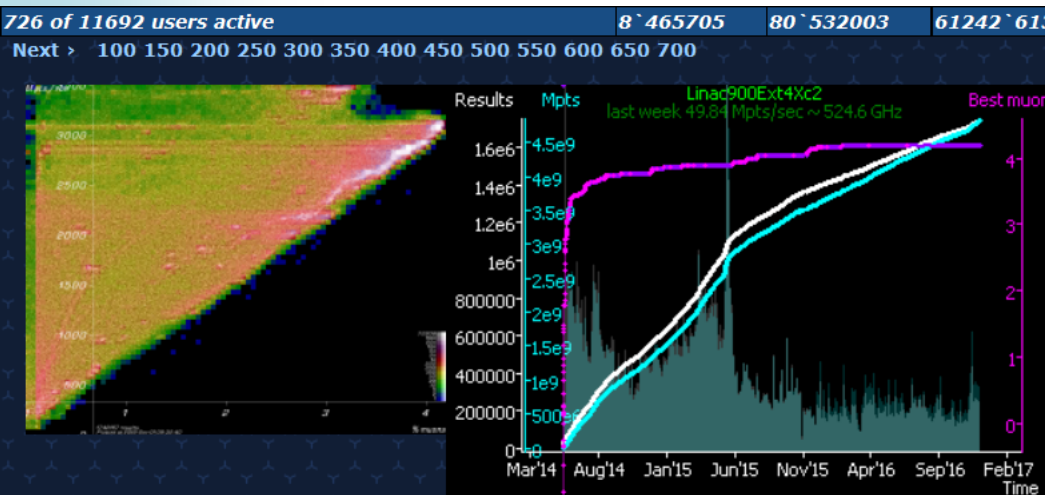
# Multi-Channel Power Supply

- Generic rack power supply
  - >\$1000 for one channel
- My monitor
  - \$699 for 11M channels
    - 2560\*1440\*3
  - \$0.000063 per channel
- Factor of  $>10^7$  is available if all you want is a large number of independent outputs
  - Via mass production, lithography industry etc.



# Automated Design: Muon1

Optimisation of design space with 100s of parameters using a genetic algorithm and distributed computing. The same optimiser designed the ATF fixed-field line.



Linac900Ext4Xc2 Tab-separated stats list [updated 2016-Dec-01; 15:08 UTC]  
Show users active in last day, week, month, quarter, year, or ever.

#	Username	v4.4 results	Mpts	Best muon percentage %	Hours since last active
1.	[OCAU] badger	67211	186° 105231.1 (3.86%)	4.183458	0
2.	[DPC] White Panther	71611	32° 970995.6 (0.684%)	4.183205	5
3.	CloverField	1603	4° 163566.4 (0.0864%)	4.182676	14
4.	[Crunchers Inc]cswchan	18465	51° 769559.1 (1.07%)	4.181424	1d 5
5.	Boots[OCAU]	26166	69° 329152.3 (1.44%)	4.180717	11
6.	Mumps [MM] 22343 (Boinc Wrapper)	8052	28° 699688.7 (0.596%)	4.180638	1w 6d 14
8.	[ARS]GOD	80909	225° 686874.8 (4.68%)	4.180474	2w 6d 10
11.	[TA]Silverthorne	44006	120° 478849.9 (2.50%)	4.176259	7
14.	[TA]JonB	30116	81° 240721.7 (1.69%)	4.174589	1d 12
16.	AETiglathPZ [US-Distributed]	25511	67° 472784.3 (1.40%)	4.173764	1w 3d 21
660 of 4423 users active		1° 742214	4818° 448939.7 (7.87%)	4.183458	0

S.J. Brooks, "Muon capture schemes for the neutrino factory", DPhil. University of Oxford (2010)

Designs lattice starting from almost nothing: labour-saving!

# Magnet with 3D Printed Parts

S.J. Brooks *et al.*, “Production of Low Cost, High Field Quality Halbach Magnets”, Proc. IPAC 2017

- Split accuracy task into two stages

Halbach quadrupole using NdFeB, 23.6 T/m, R=34.7mm bore (0.82T max),  $10^{-4}$  errors at R=10mm

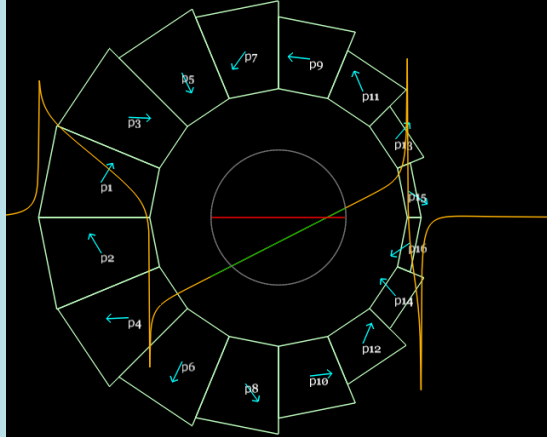


Material cost: \$1100. No alignment better than 0.25mm required anywhere. Assembled with mallet.

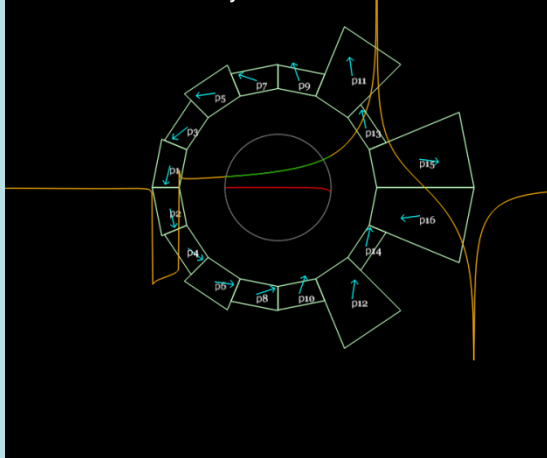


# Custom and Cheap – is it possible?

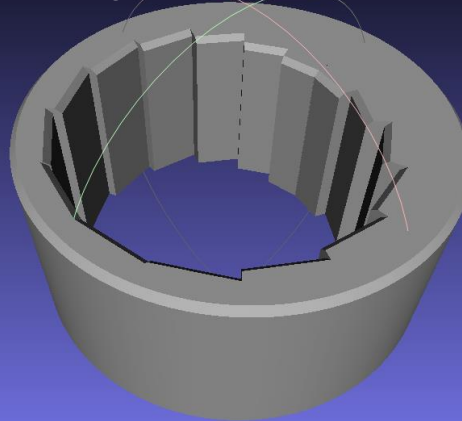
Combined function dipole+quad



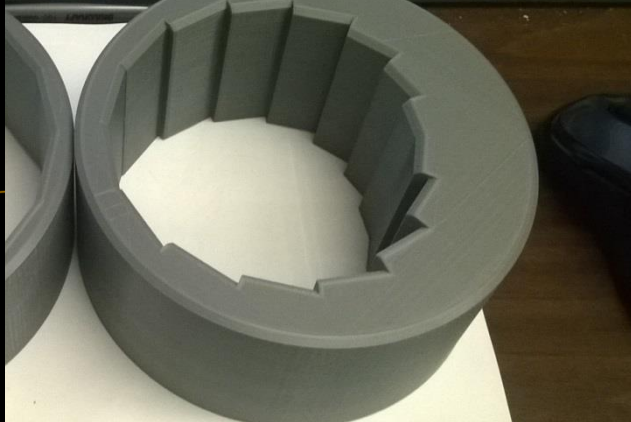
Design for  $B_y = B_0 r^k$



Magnet design program generates mesh



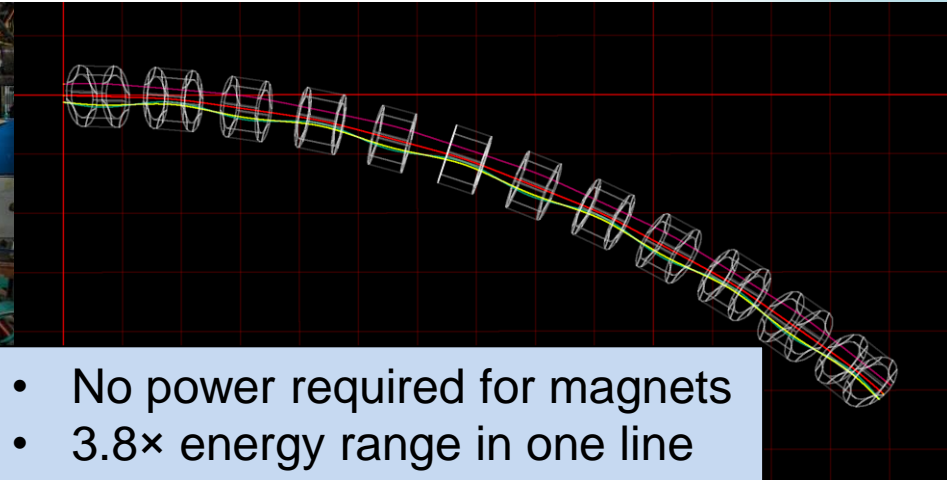
3D printed



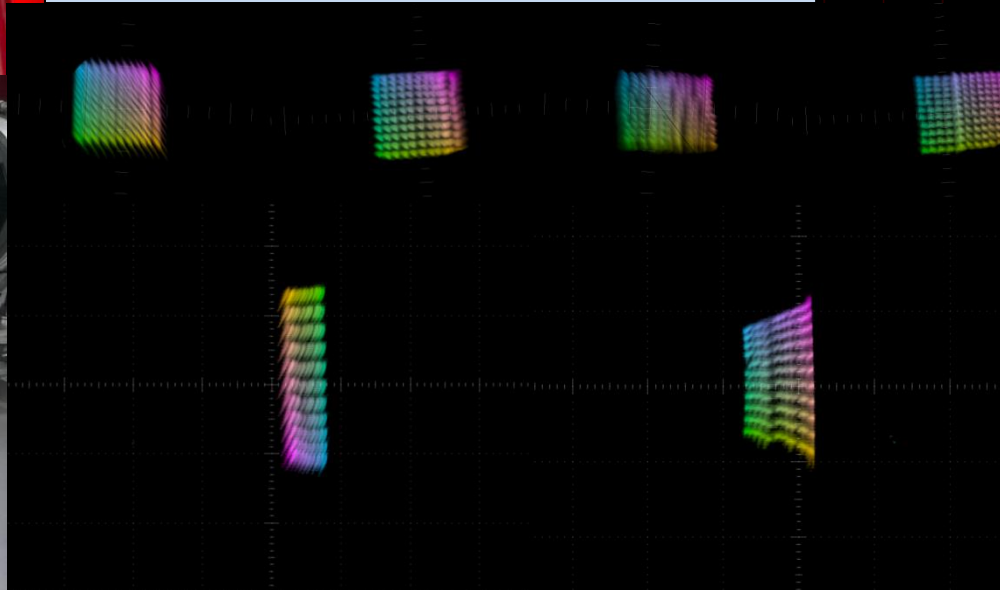
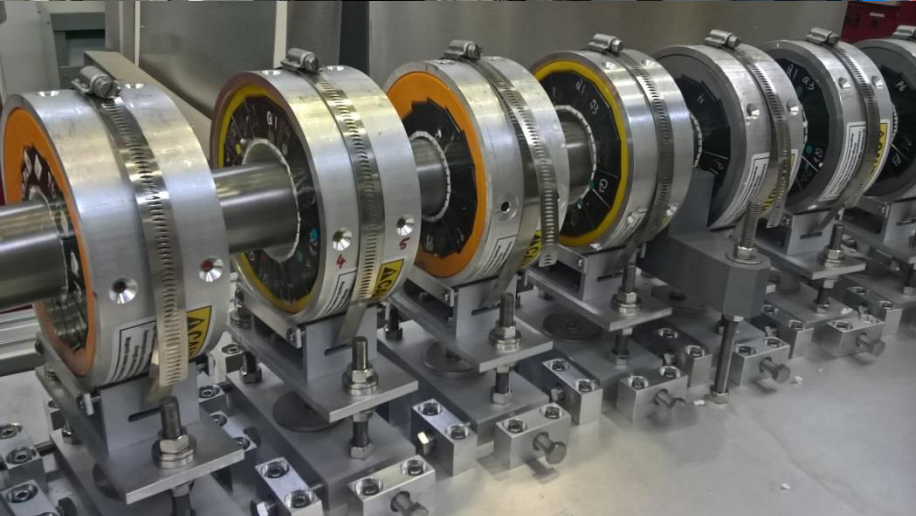
Material cost: \$800

# ATF1 Fixed-Field Arc Test (AE79)

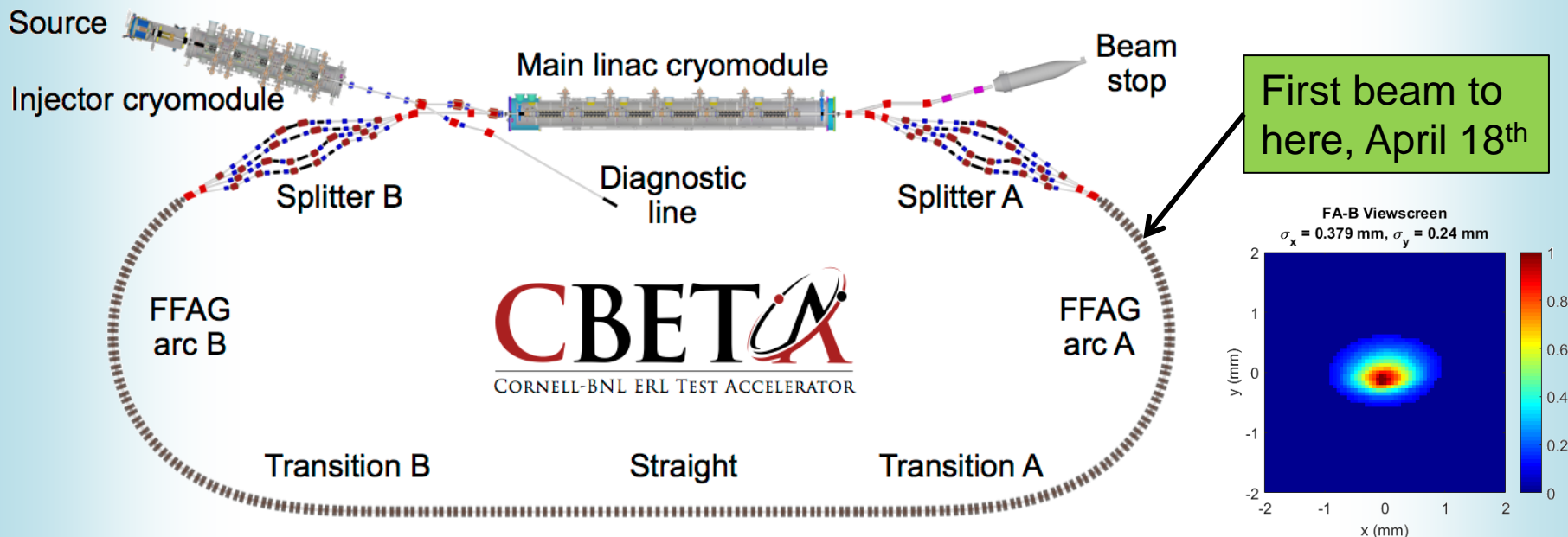
S.J. Brooks, talk at FFAG 2017 workshop



- No power required for magnets
- $3.8\times$  energy range in one line



# Re-use/Recycle: CBETA ERL



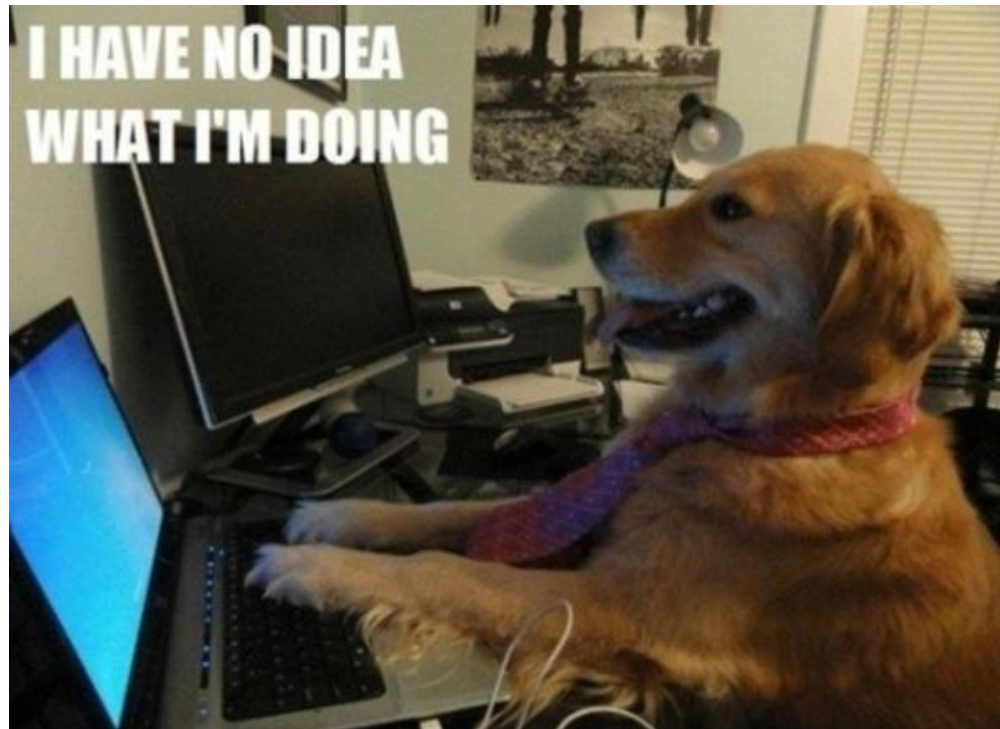
- Superconducting linac module
  - With energy recovery ( $150\text{MeV} \cdot 40\text{mA} = 6\text{MW}$  power in beam, 45kW of actual RF amplifiers)
  - 36MeV energy gain module used 4 times (more energy per hardware)
- Permanent magnet recirculating lines (low/zero power)
  - Used multiple times in fixed-field optics (4 energies in one line, CW)

# BACKUP



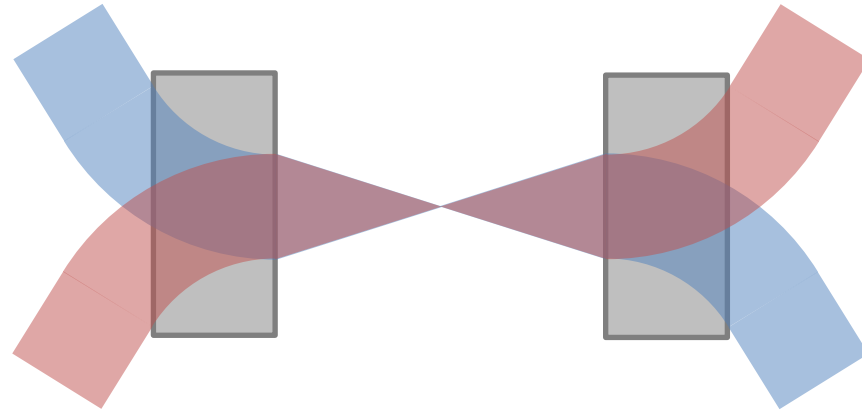
# Warning

- Lots of this talk is speculative





# Neutralised Focus: Solution in Search of a Problem



- No good for beam-beam limit
  - Instability governed by  $d\text{Force}/dx$  not size of Force
- Probably no good for fusion (ICF)
  - Requires awkward energy recovery system
- Maybe can make dense/degenerate matter?

# Generalised Halbach design

My current sheet approximation code (PM2D) is good enough



Material grade: N35SH from AllStar Magnetics,  $B_r(\text{eff.})=1.194\text{T}$

# Best so far: QF3

Table 1: Field harmonics from ERHIC-PMQ\_0503\_0004\_001 at R=10mm. The nominal magnet length is 57.4412mm and the average field corresponds to 23.6386 T/m.

Field harmonic	Normal units	Skew units
Dipole	0.00	-0.00
Quadrupole	10000.00	0.00
Sextupole	-0.18	-0.94
Octupole	0.34	0.17
Decapole	-0.65	0.09
Dodecapole	-0.05	0.02
14-pole	-0.02	-0.01
16-pole	-0.00	0.00
18-pole	0.00	0.00
20-pole	-0.00	-0.00
22-pole	-0.00	-0.00
24-pole	-0.00	0.00
26-pole	0.00	-0.00
28-pole	0.00	-0.00
30-pole	-0.00	-0.00

# Cost and Labour per Magnet

- Permanent magnet wedges (AllStar N35SH)
  - \$1052.67 per QF magnet (16 wedges)
  - \$758.00 per BD magnet (16 wedges)
- Labour ~8h per magnet: 3h measurement, 2h shimming, 2h assembly, 1h 3D printer setup
- Required infrastructure
  - 3D printer (\$2-3k), used Ultimaker 2 Extended+
  - Rotating coil (~\$50k)

# Benefits

- No power consumption
  - No power supply, no copper wires or windings
- Any field shape you like within strength limits
- No “cross-talk” between iron surfaces in compact lattices
- Can be assembled with mallet
- $1e-4$  accuracy is possible after shimming
- Seems cheap, at least for short magnet length