

Scaling VFFAG eRHIC Design

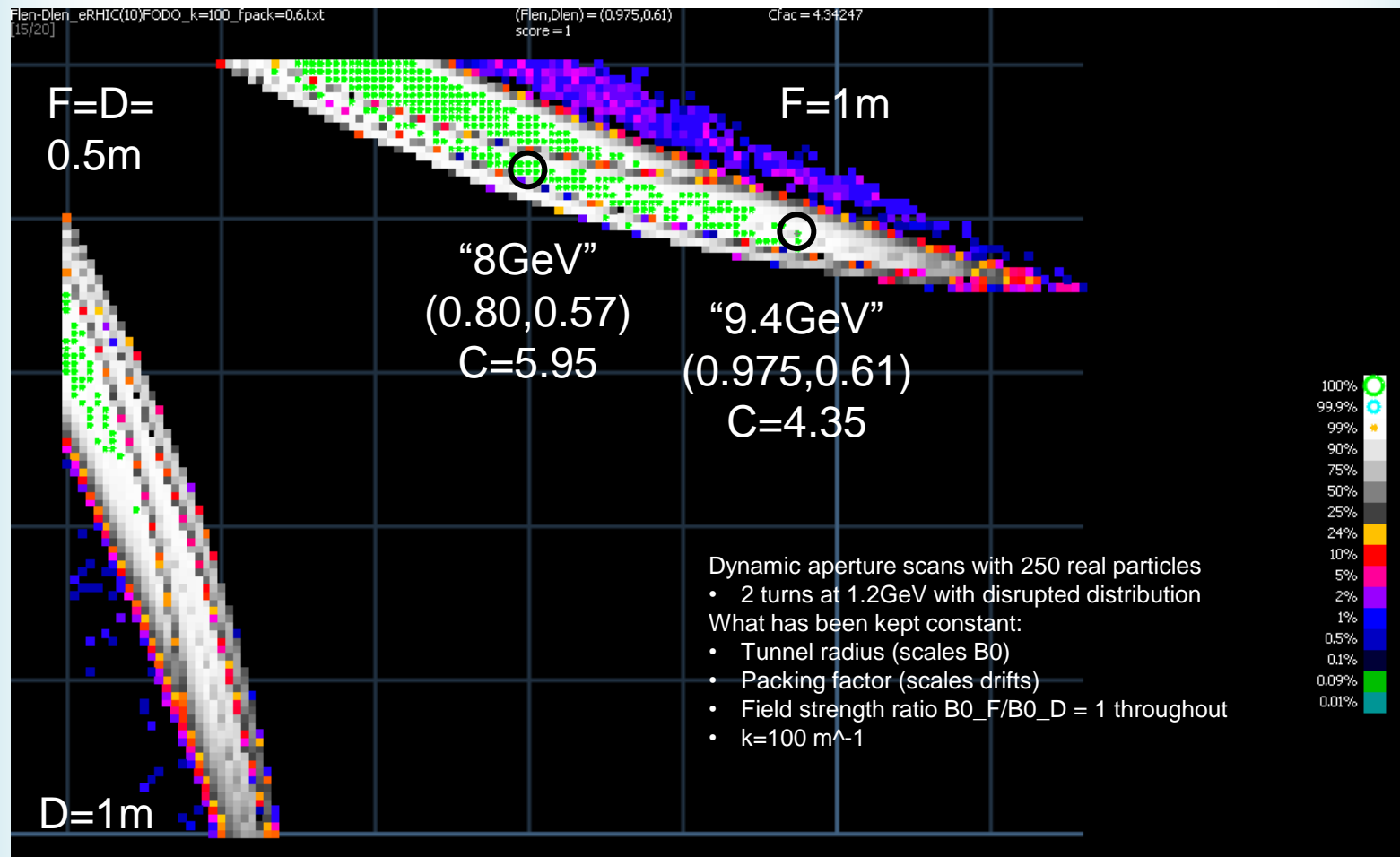
Progress Report 3

Last time:

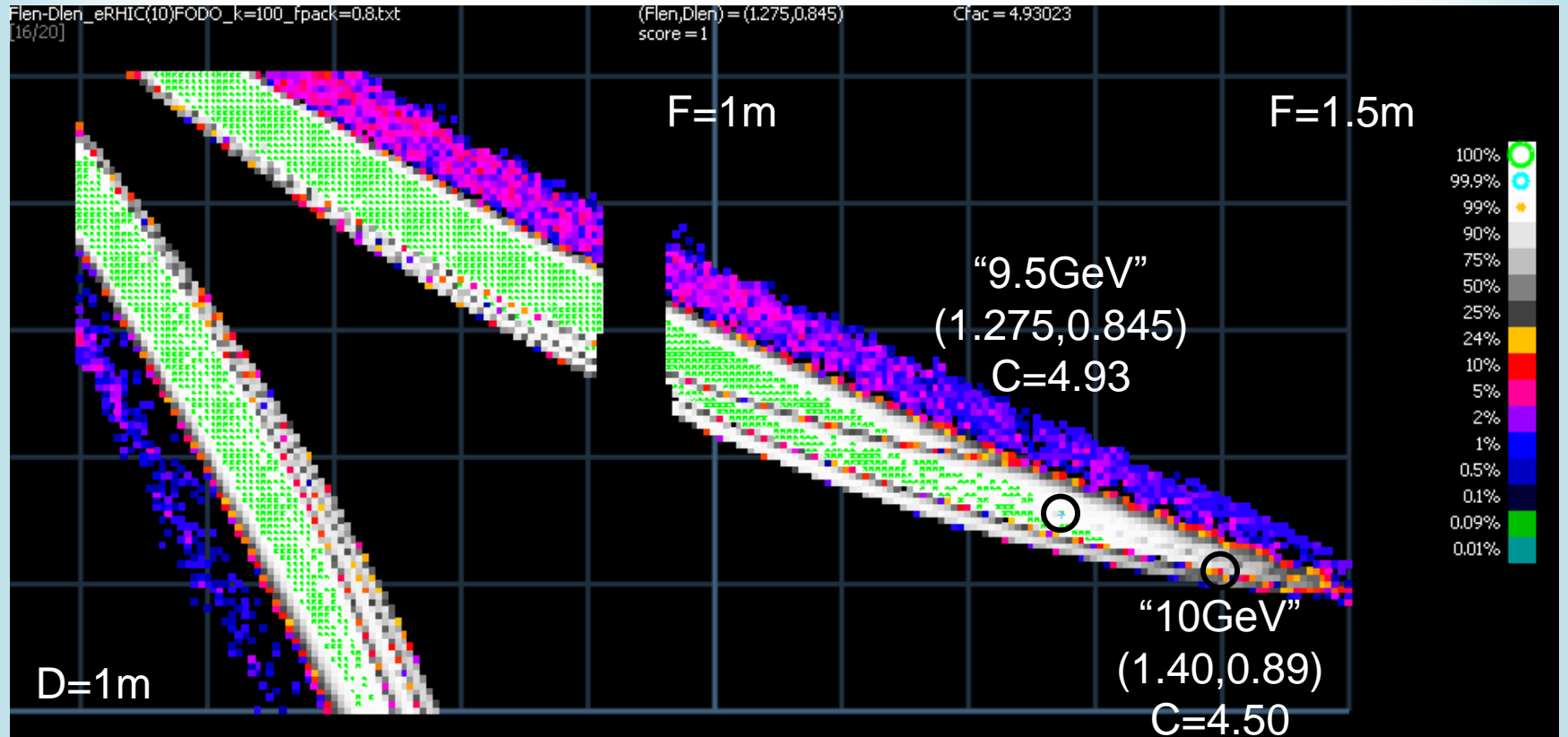
- Found FODO lattices capable of 8 and 10GeV
 - 8GeV lattice very robust
 - Orbit excursion of 3cm without errors seemed possible
 - 10GeV lattice exhibited resonance behaviour
- Running long dynamic aperture scans of FODO stability for 60% and 80% packing factor

I. FODO Parameter Space & 9.4/9.5GeV Lattices

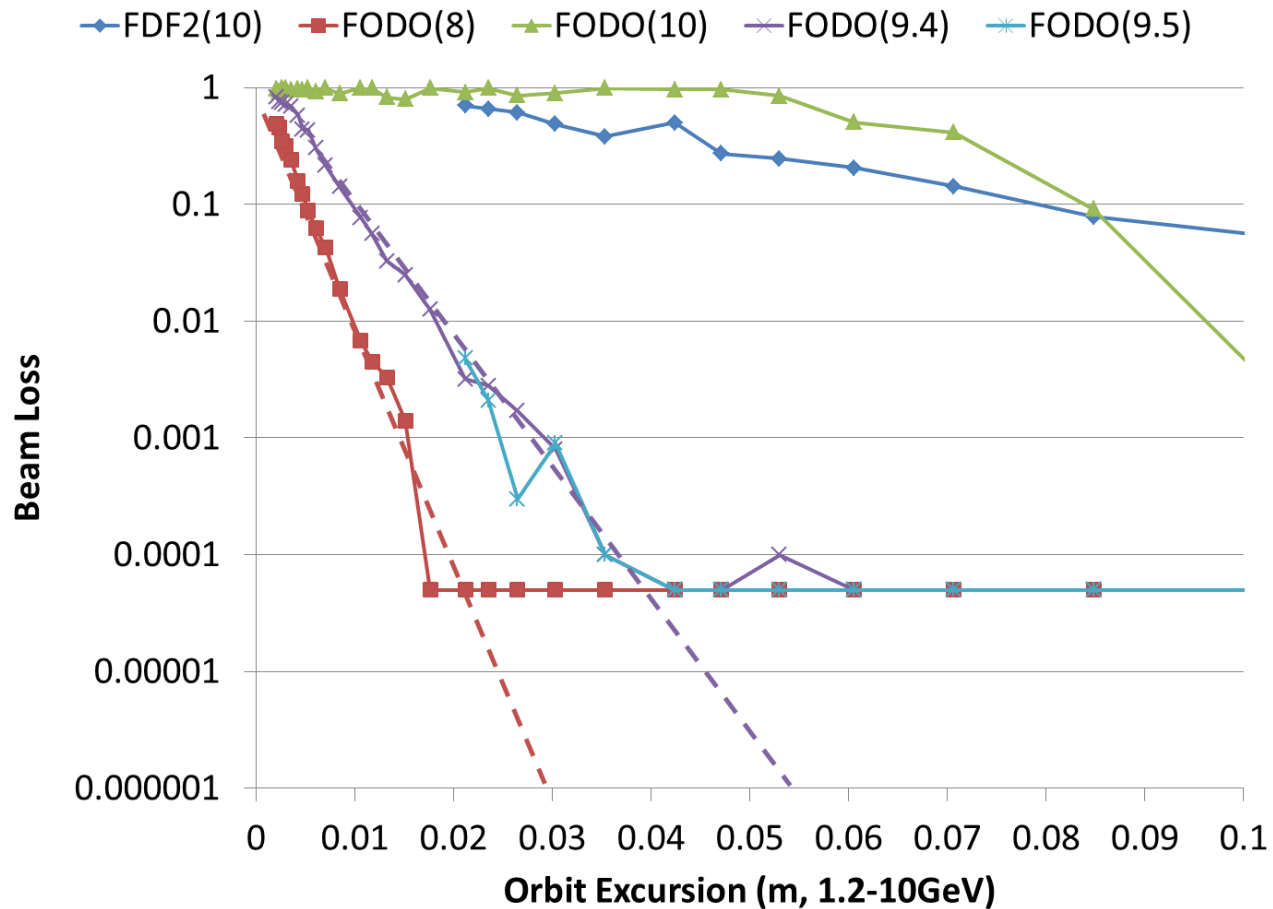
FODO lattice, 60% packing factor



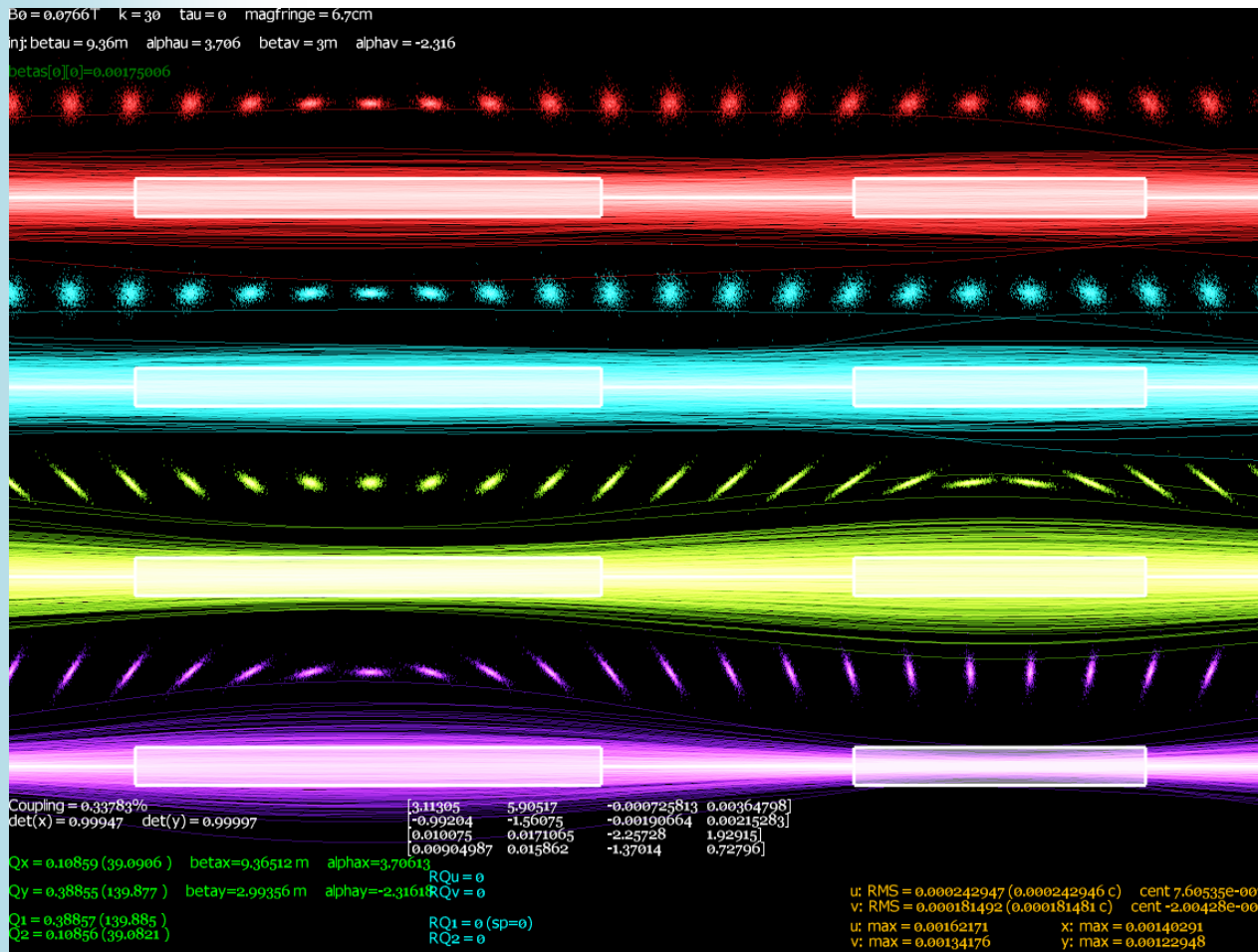
FODO lattice, 80% packing factor



Loss performance with scaling k



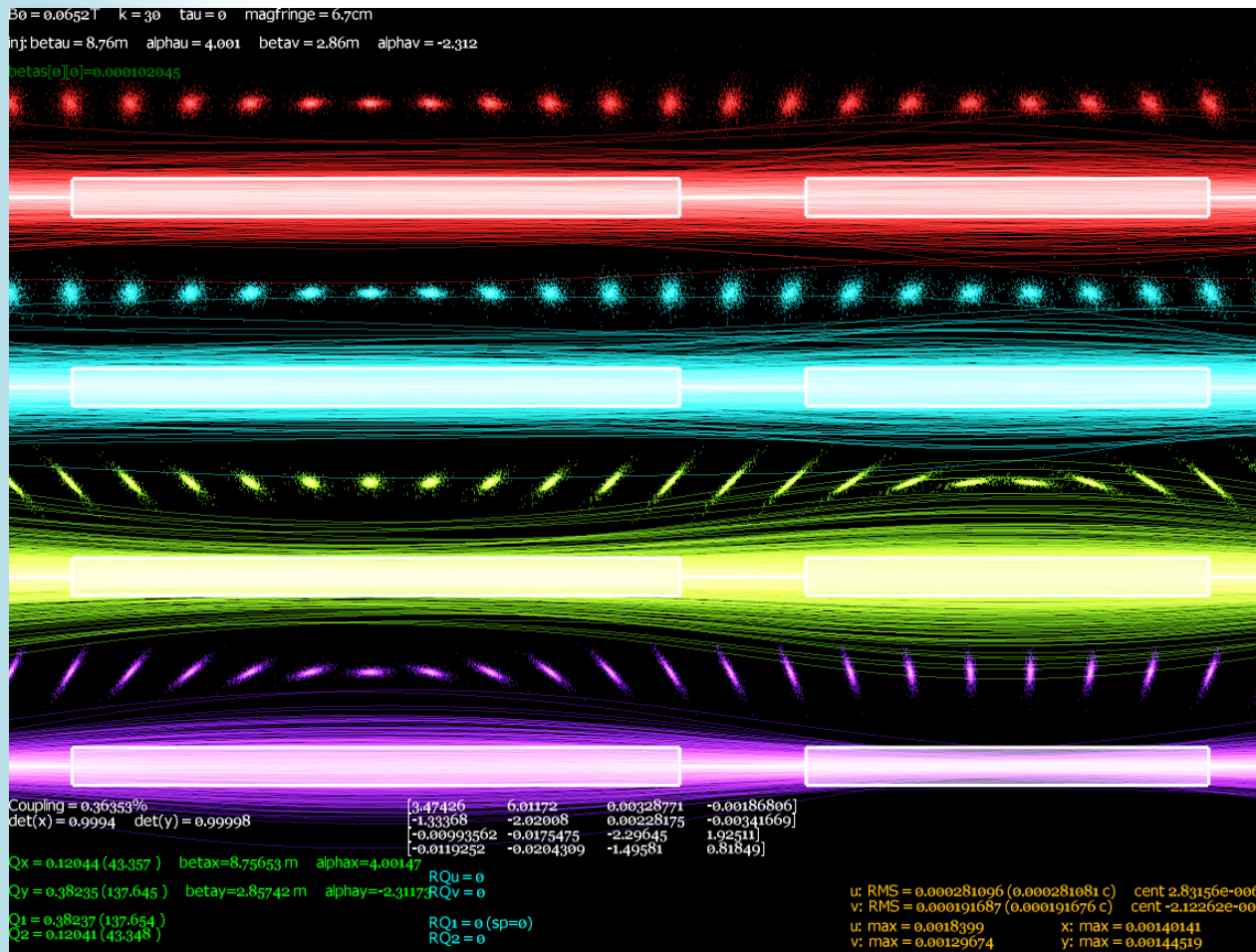
9.4GeV/60% pack FODO lattice



Species: Electrons
 Injection energy (MeV): 1200
 Extraction energy (MeV): 9400
 Lattice: FODO
 Magnet B_0 (T): 0.0766
 Magnet k (m^{-1}): 30
 Magnet τ : 0
 Magnet fringe length (m): 0.067
 F Magnet length (m): 1.78
 D Magnet length (m): 1.114
 Drift length (m): 0.965
 Injected normalised emittance (m.rad):
 19.36381158822e-6
 Injected β_u (m): 9.36
 Injected β_v (m): 3
 Injected α_u : 3.706
 Injected α_v : -2.316
 Injected distribution: ExpTails
 Designed for tracking in: S

Cell length = 4.824 m
 Orbit excursion = 0.0686006 m
 Bending radius = 378.66 m
 Packing factor = 0.59992
 Circumference factor = 4.34535
 $E_{\text{max_eRHIC}} = 9.47752\text{ GeV}$

9.5GeV/80% pack FODO lattice



Species: Electrons
 Injection energy (MeV): 1200
 Extraction energy (MeV): 9500
 Lattice: FODO
 Magnet B_0 (T): 0.0652
 Magnet k (m^{-1}): 30
 Magnet τ : 0
 Magnet fringe length (m): 0.067
 F Magnet length (m): 2.328
 D Magnet length (m): 1.543
 Drift length (m): 0.484
 Injected normalised emittance (m.rad):
 19.36381158822e-6
 Injected β_u (m): 8.76
 Injected β_v (m): 2.86
 Injected α_u : 4.001
 Injected α_v : -2.312
 Injected distribution: ExpTails
 Designed for tracking in: S

Cell length = 4.839 m
 Orbit excursion = 0.0689533 m
 Bending radius = 378.603 m
 Packing factor = 0.79996
 Circumference factor = 4.93121
 $E_{\text{max_eRHIC}} = 9.55964 \text{ GeV}$

Tunes

Lattice	Qu (deg)	Qv (deg)	Qu	Qv
FDF2(10)	82.7	255.5	0.230	0.710
FODO(8)	64.3	133.6	0.179	0.371
FODO(10)	41.1	158.5	0.114	0.440
FODO(9.4)	39.1	139.9	0.109	0.389
FODO(9.5)	43.4	137.6	0.120	0.382

II. Synchrotron Radiation Power

SR in arcs for 50mA, sum all turns

Top Energy (GeV)	Turns	Linac (GeV)	FODO 9.4GeV/60%	FODO 9.5GeV/80%
10	9	1.1	13.64 (MW)	13.17 (MW)
10	8	1.2375	12.18	11.77
10	7	1.4143	10.74	10.38
10	6	1.65	9.31	9.00
9.5	9	1.0444	11.11	10.74
9.5	8	1.175	9.93	9.59
9.5	7	1.3429	8.75	8.46
9.5	6	1.5667	7.59	7.33
9	9	0.9889	8.96	8.65
9	8	1.1125	8.00	7.73
9	7	1.2714	7.06	6.82
9	6	1.4833	6.12	5.91

III. Arc Magnets Specification

Use FODO 9.5GeV/80% lattice

- $B_y = B_0 e^{ky}$ (and $B_x = 0$) for $x = 0$
 - $k = 30\text{m}^{-1}$, $B_0 = 0.0652\text{T}$ (field at 1.2GeV)
- $B_y = 0.5160\text{T}$, $y = 68.95\text{mm}$ at 9.5GeV
- $B_y = 0.7604\text{T}$, $y = 81.88\text{mm}$ at 14GeV
 - Use for high energy, reduced current operation
- Good field region x : -3 to 3mm, y : -3 to 83mm
- F, D magnet lengths: 2.328m, 1.543m
- 61.418m radius of curvature ($B_{0_D} = -B_{0_F}$)

IV. Future Work

Next steps (roughly in this order)

- Redo simulations with weighted particles in tails (down to $1e-6$ and beyond)
- Error (misalignment) study
 - Include logs of emittance growth, centroid offset
- Develop “straight” cell for full ring lattice
- Open issue concerning emittance growth from synchrotron photon emission
- “End-to-end” tracking of full ring